

Lecture Notes

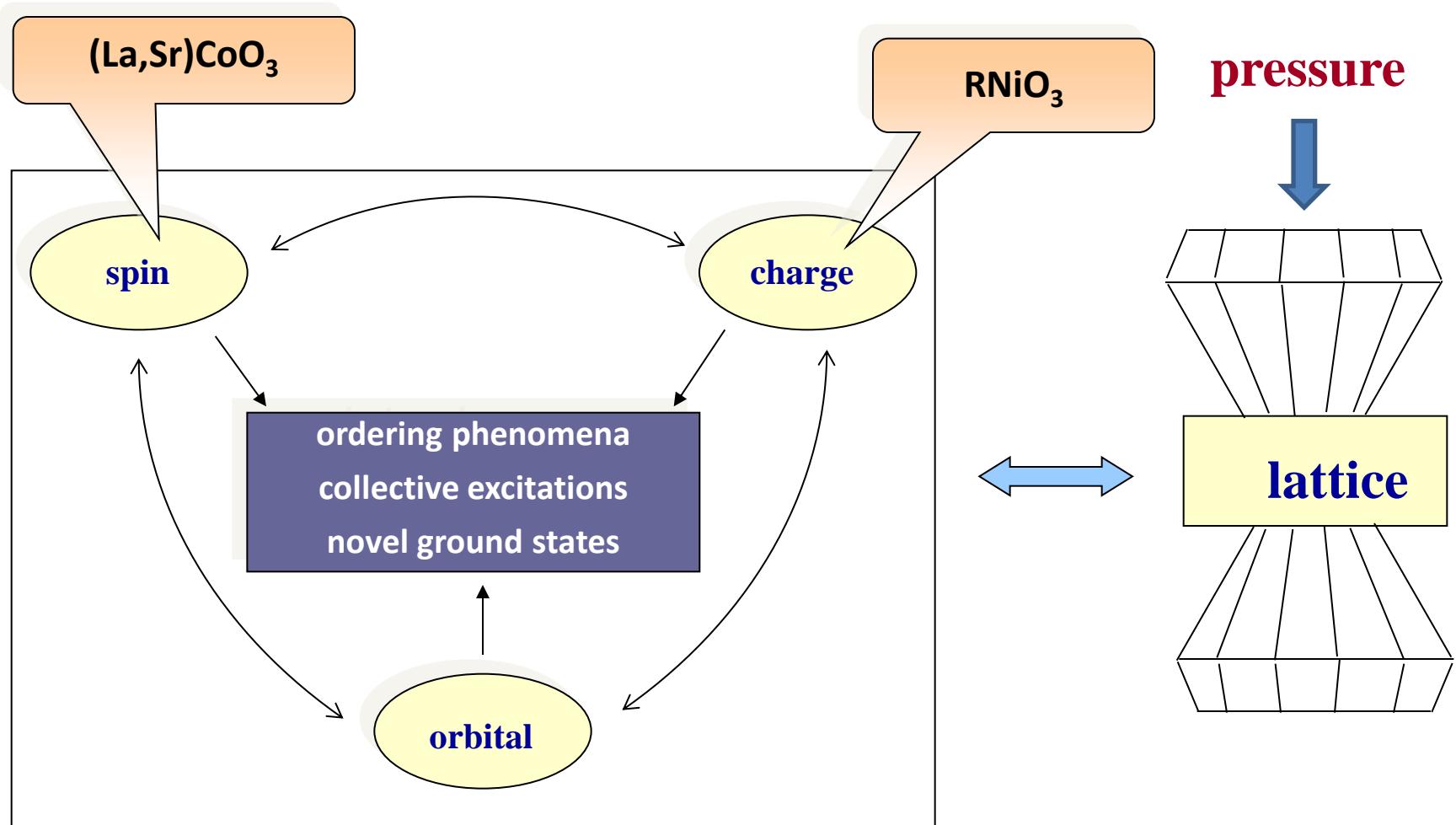
Introduction to Strongly Correlated Electron Systems

WS 2014/ 2015

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Selected correlated oxides



Investigation of the mechanism of the metal insulator transition!

Strongly correlated transition metal systems

Recent high pressure studies:



TiOCl: low dimensional spin 1/2 system (Ti^{3+} ; $3d^1$) Mott insulator

**Metal Cluster compounds: AM_4X_8 (A=Ga; M=Nb,Ta; X=S,Se)
a new class of Mott insulators**

TiOCl

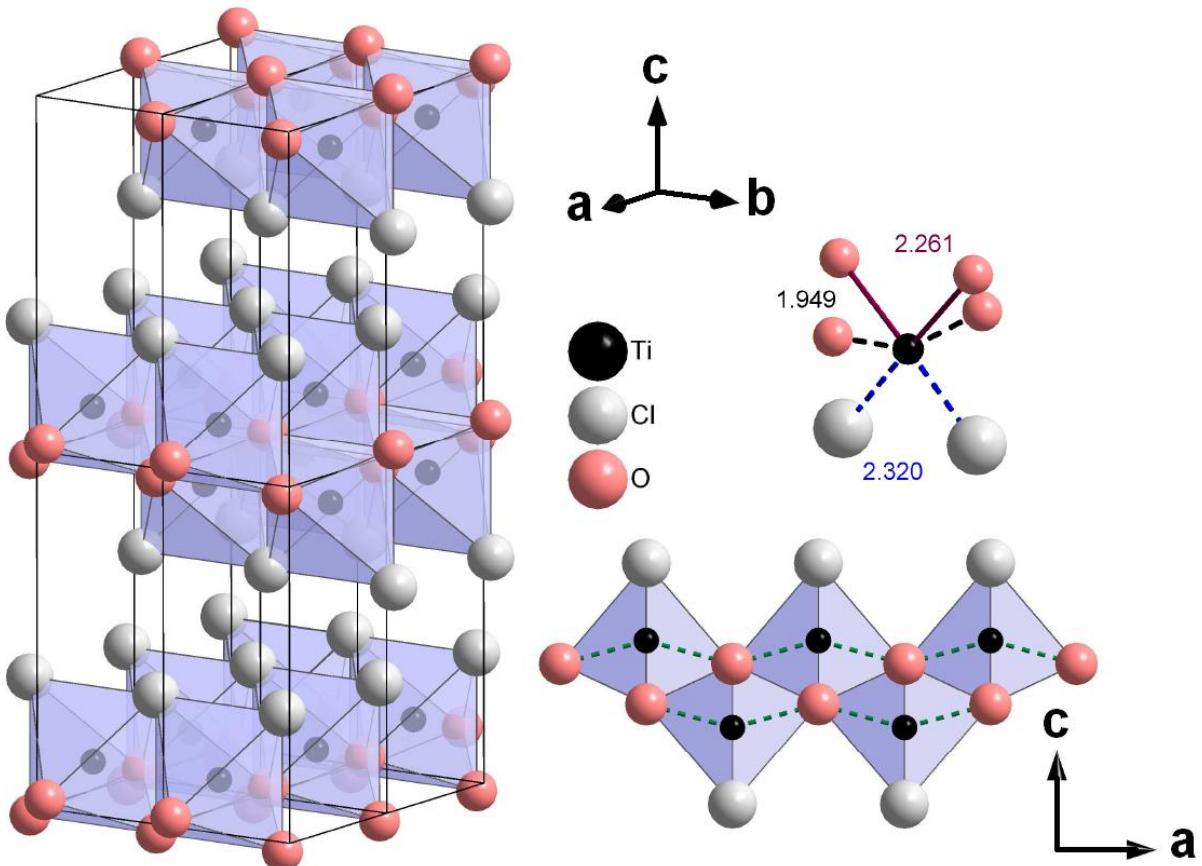
University of Cologne: structural and transport properties

M. K. Forthaus, D. I. Khomskii, A. Möller, T. Taetz, MMA

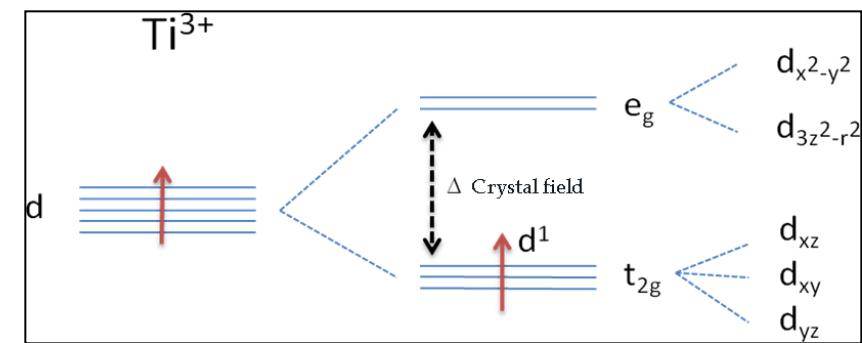
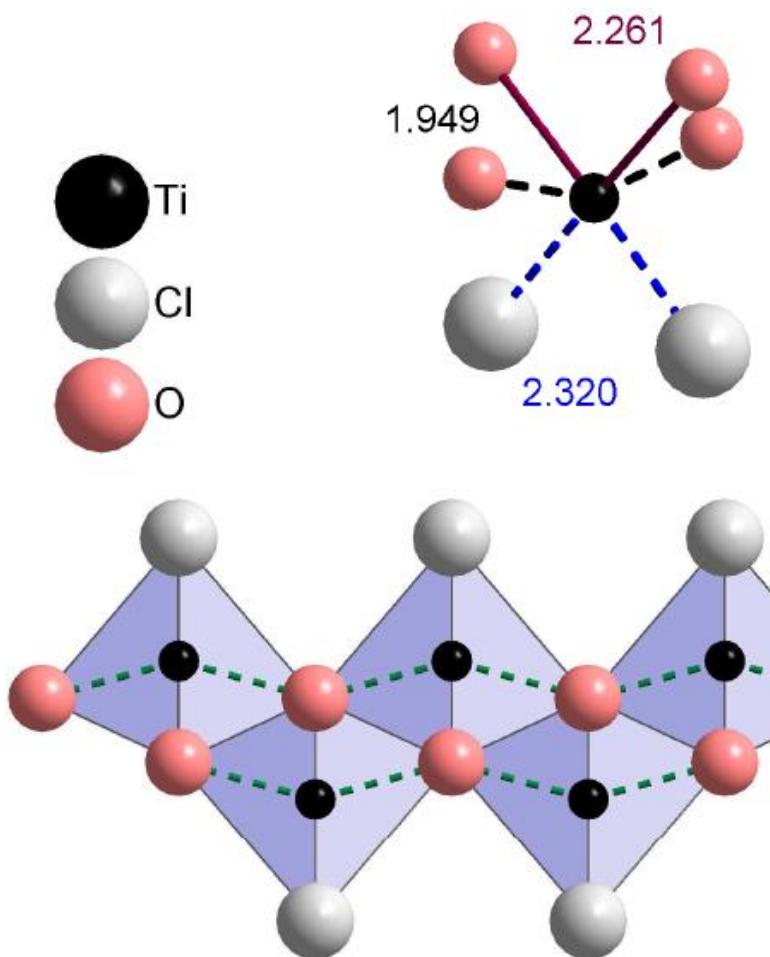
Universidad de Santiago de Compostela: structural, magnetic properties, and theoretical description

S. Blanco-Canosa, F. Rivadulla, A. Piñeiro, V. Pardo, D. Baldomir, M. A. López-Quintela

TiOCl – structural properties



- orthorhombic FeOCl-structure (*Pmmn*)
- separated bilayers of TiO_4Cl_2 -octahedra
- Formation of Ti^{3+} -chains along **b**-axis ($\text{Ti}^{3+} \Rightarrow 3d^1$)
- spin-1/2-chains weakly coupled by O^{2-} -chains



TiOCl – magnetic properties

- high temperatures:

Heisenberg AF ($J \sim 660\text{K}$)

- at $T_{c2} = 92\text{ K}$: phase

transition (second order,

Hemberger et al., PRB (2005))

- $T_{c1} < T < T_{c2}$: incommensurate

phase due to interchain

frustration (Rückamp et al.,

PRL (2005))

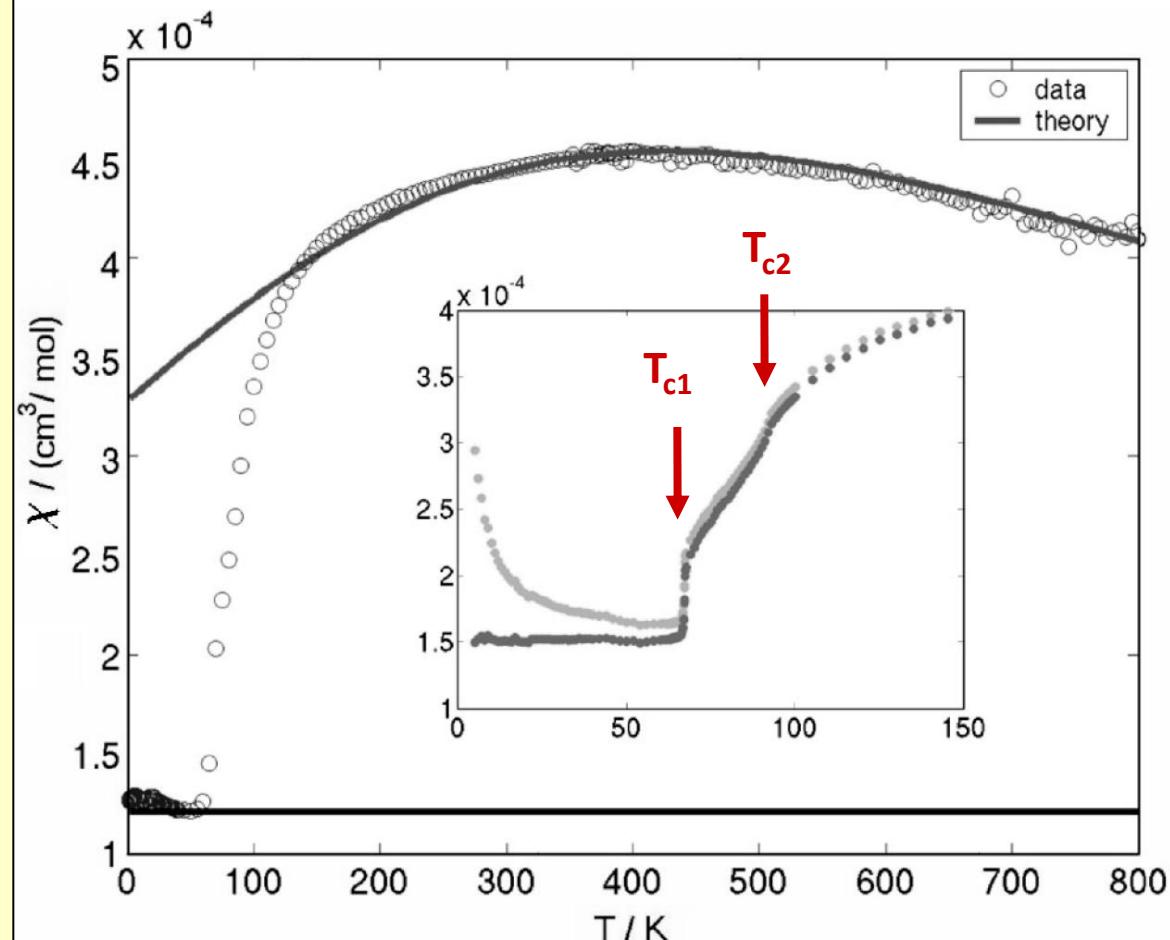
- at $T_{c1} = 67\text{ K}$: phase

transition to nonmagnetic

state (spin-Peierls transition)

- $T < T_{c1}$ dimerized

commensurate phase



What is **Spin-Peierls** transition?
See board!

First **Peierls** transition

Peierls transition

Metal \rightarrow insulator transition which occurs in 1-dimension metals with $1/2$ filled band

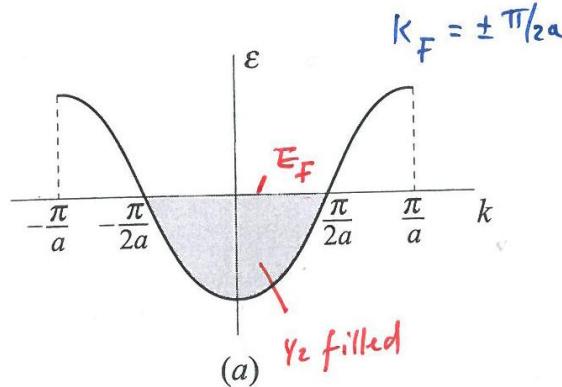
origin: a structural transition (distortion) which leads to a doubling of the unit cell
 \Rightarrow dimerization!

- How lattice distortion leads to electron energy gain and gap?

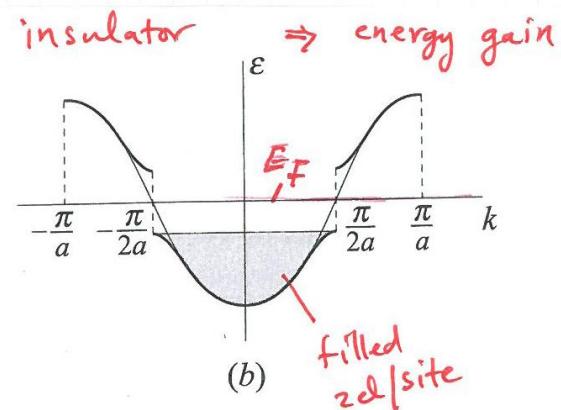
Consider 1-d chain with 1 electron / site and treat the electrons in the TB-approx.

\Rightarrow Energy spectrum $E(k) = -2t \cos k\alpha$ (t = electron-electron hopping, a lattice period)

Metal



insulator



Lattice periodicity $\overset{\sim}{\circ} \circ \circ \circ \circ \circ$

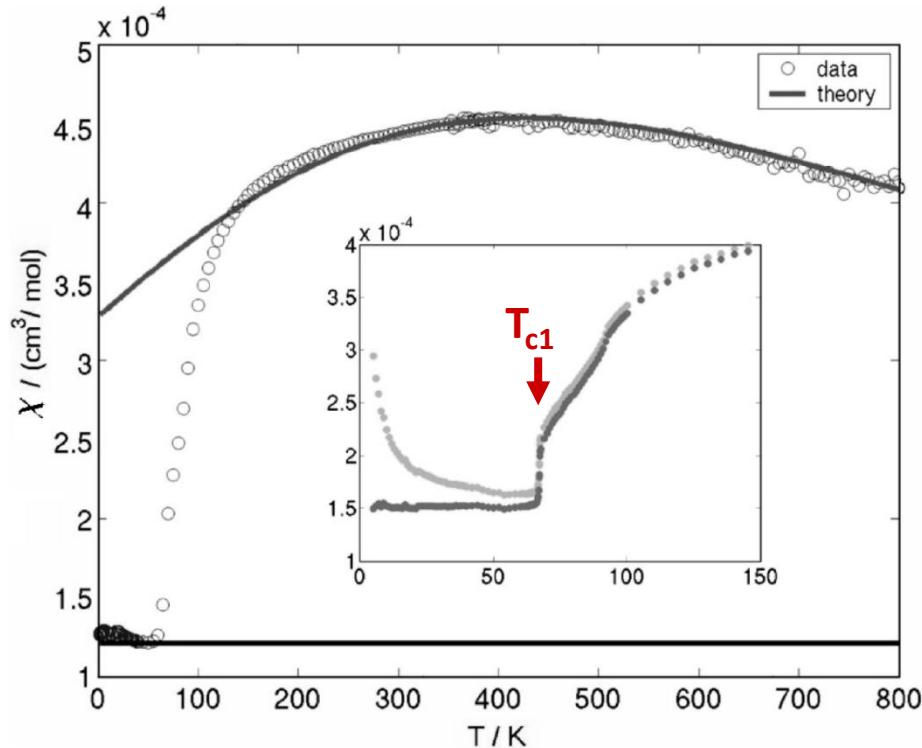
$\overset{\sim}{\leftrightarrow} \leftrightarrow \leftrightarrow \leftrightarrow \leftrightarrow \leftrightarrow$

Electron energy gain, but we have to deform the lattice \Rightarrow elastic energy of a lattice distortion U is $\sim U^2$. However energy gain $\sim U^2 / nU$

\Rightarrow Electron energy gain always exceeds the elastic energy loss!

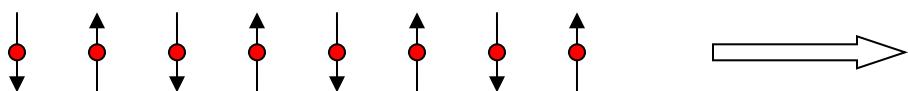
TiOCl: low-temperature phase

dimerization and magnetoelastic coupling → spin-Peierls instability !

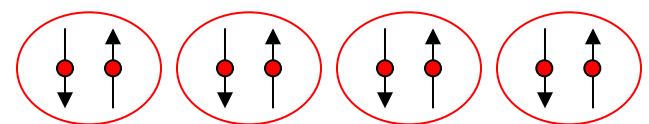


-at $T_{c1} = 67 \text{ K}$: phase
transition to nonmagnetic
state (spin-Peierls transition)
- $T < T_{c1}$ dimerized
commensurate phase

Spin-Peierls phase



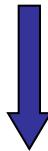
$S=1/2$ antiferromagnetic chain



→ formation of spin singlets $S=0$

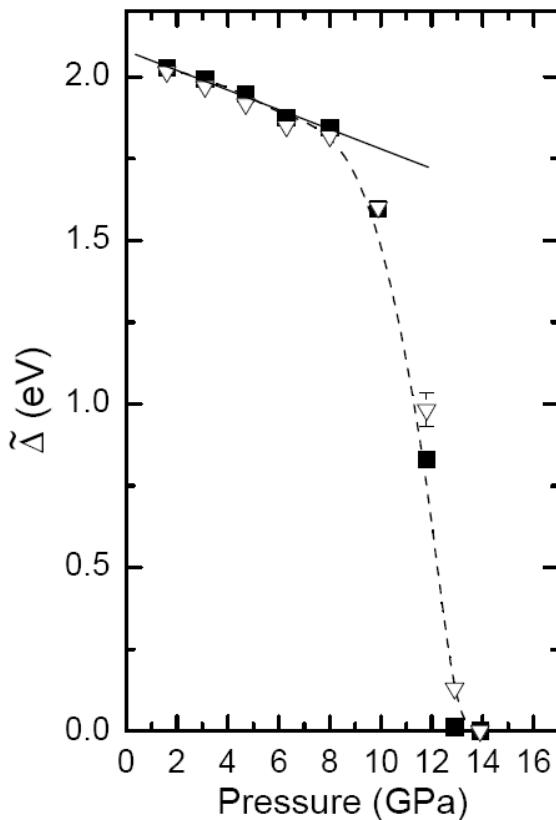
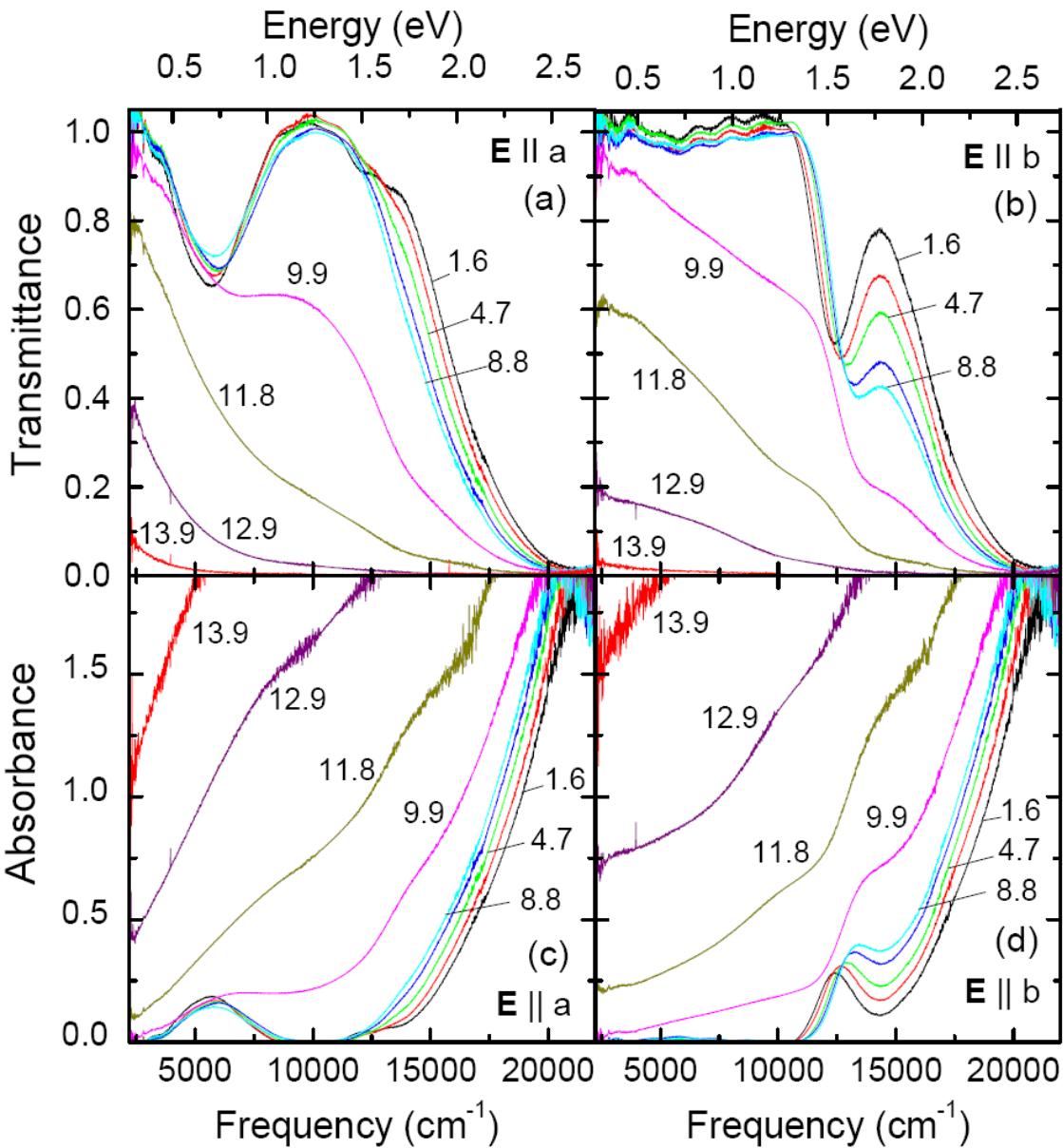
TiOCl – interesting aspects

- low dimensional spin 1/2 system (Ti^{3+} ; 3d¹)
→ S=1/2 layered Mott insulator
- strong coupling of 1D antiferromagnetic chains to the lattice
→ spin-Peierls transition and simultaneous lattice dimerization of Ti^{3+} ions



⇒ Promising system for the investigation of pressure-induced metal insulator transitions

effect of pressure on optical properties



Possible metal insulator
transition at ~ 12 GPa !

C.A. Kuntscher et al. PRB (2008):
connected to structural phase
transition!

aim of this work

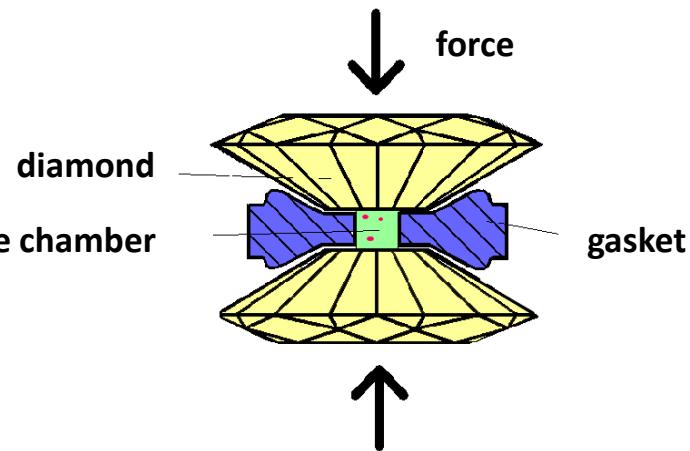
Effect of pressure on the electrical transport and structural properties of TiOCl

Experimental techniques:

- electrical resistivity up to ~ 25 GPa
- x-ray diffraction:
 - energy dispersive XRD up to ~ 8 GPa (MAX 80) / ~ 17 GPa
 - **angle dispersive XRD up to ~ 15 GPa**
- EXAFS (Ti K edge) up to ~ 20 GPa
- **magnetic susceptibility up to 1 GPa (teflon cell in SQUID)**

Experimental setup: Diamond Anvil Cell

x-ray diffraction



sample chamber $\varnothing = 100 - 300\mu\text{m}$;

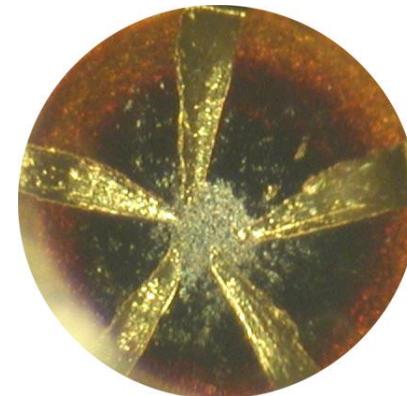
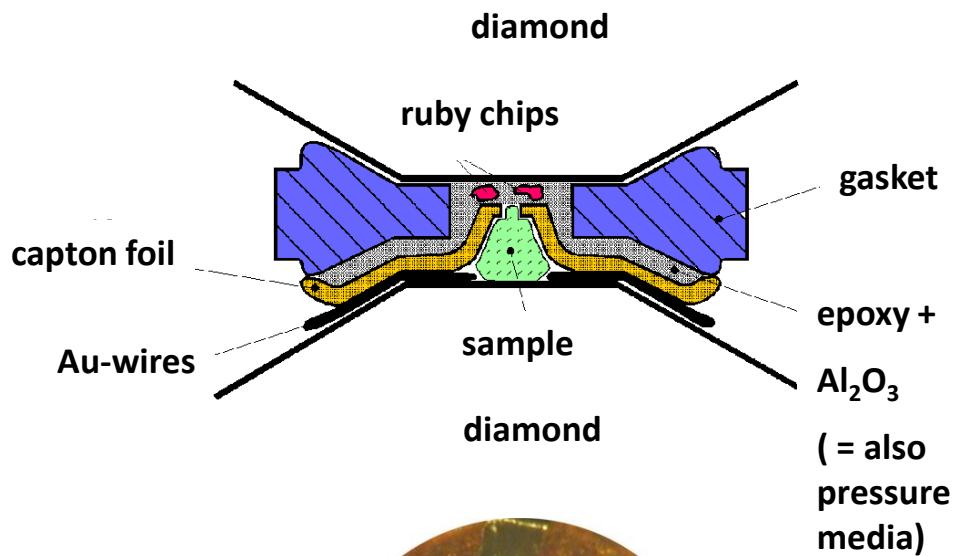
height: 25-50 μm

$p_{\max} \approx 100 \text{ GPa} (= 1 \text{ Mbar})$

Pressure media: e.g. **Methanol:Ethanol 4:1**, liquid

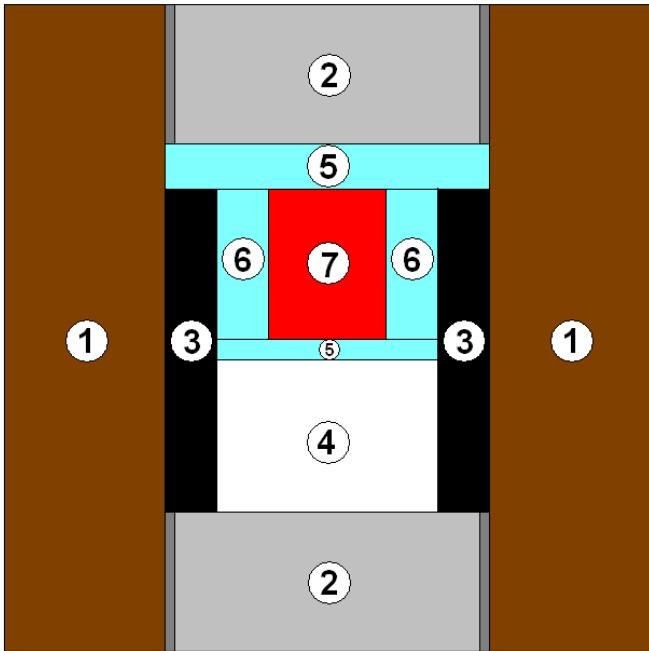
Nitrogen, liquid Argon, liq. Helium, Oil, Epoxy, etc.

resistivity measurements

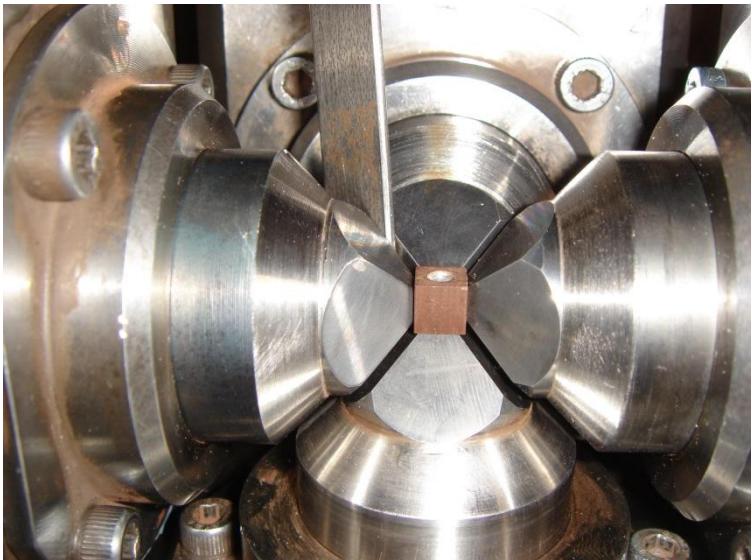


sample chamber $\varnothing \approx 100 \mu\text{m}$

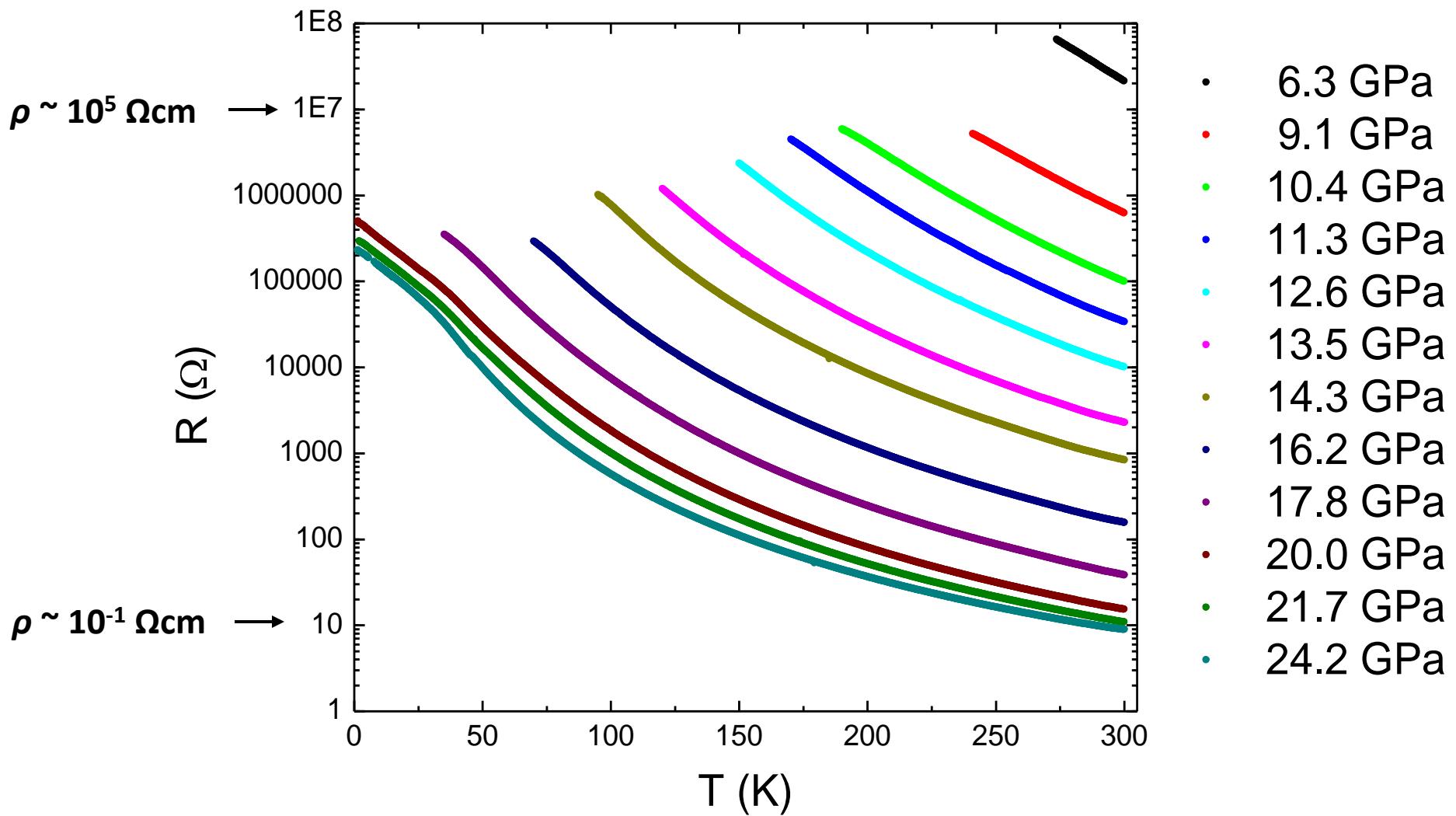
Experimental setup: MAX 80 at F2.1, HASYLAB



- 1) Boron-Epoxy cube
- 2) steel-ring with pyrophilite
- 3) graphite cylinder
- 4) NaCl
- 5) BN powder
- 6) BN cylinder
- 7) SAMPLE

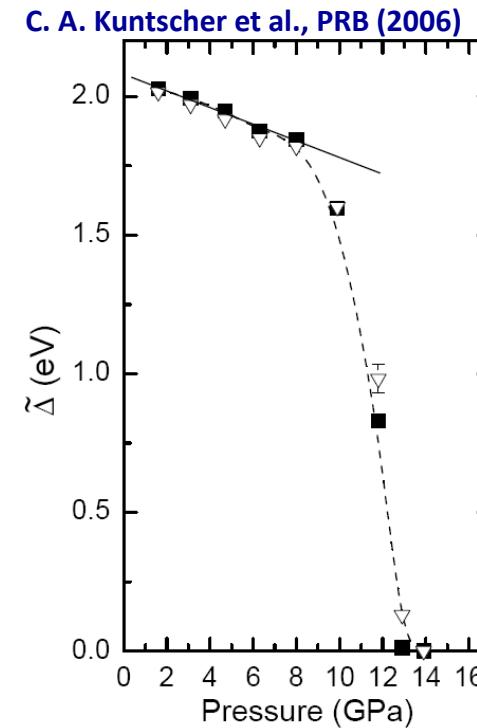
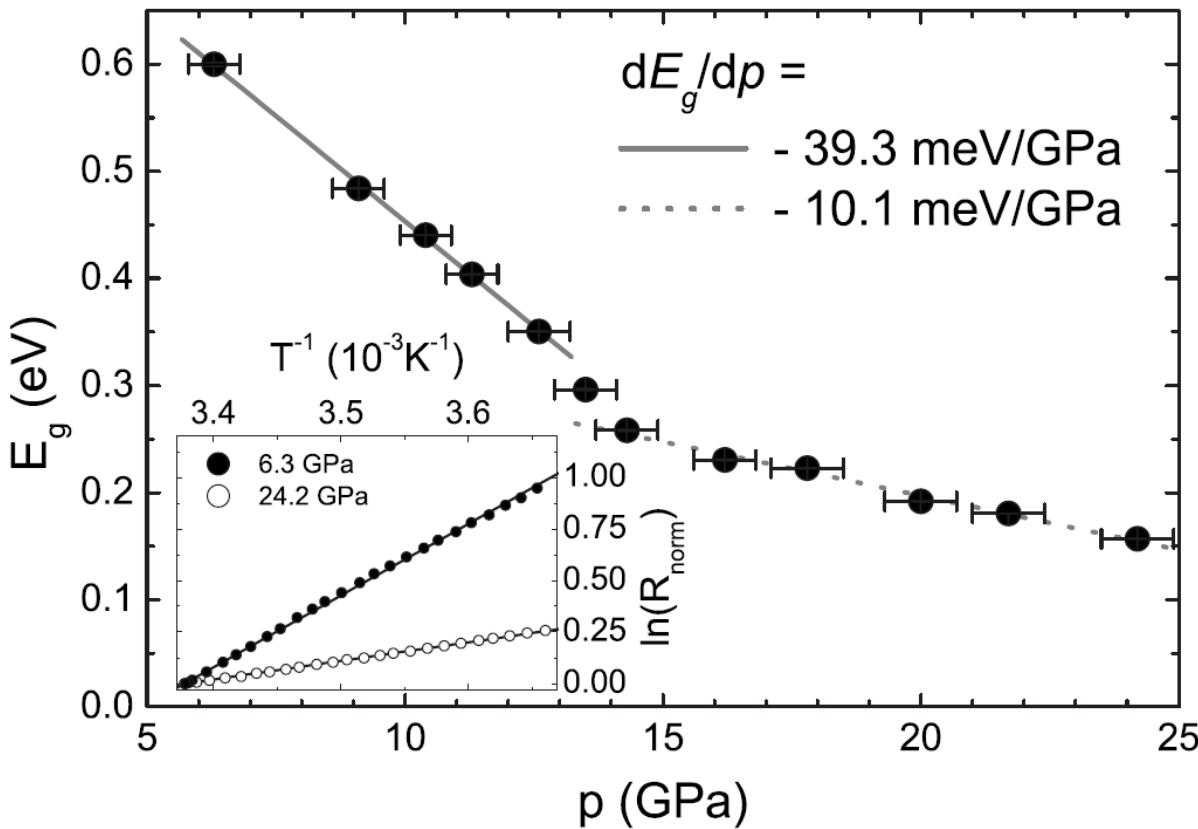


electrical transport under pressure



- dramatic reduction of R_{294K} with pressure - more than 6 orders of magnitude
- Temperature dependence: no metallic behaviour up to 24.2 GPa

energy gap $E_g(p)$ at room temperature



abrupt change of pressure dependence of $E_g(p)$ at $\sim 12 \text{ GPa}$:
Slope of $E_g(p)$ decreases by a factor of 4!

- drastic change of the electronic properties above 12 GPa !
➤ but no metallic state up to $\sim 24 \text{ GPa}$!

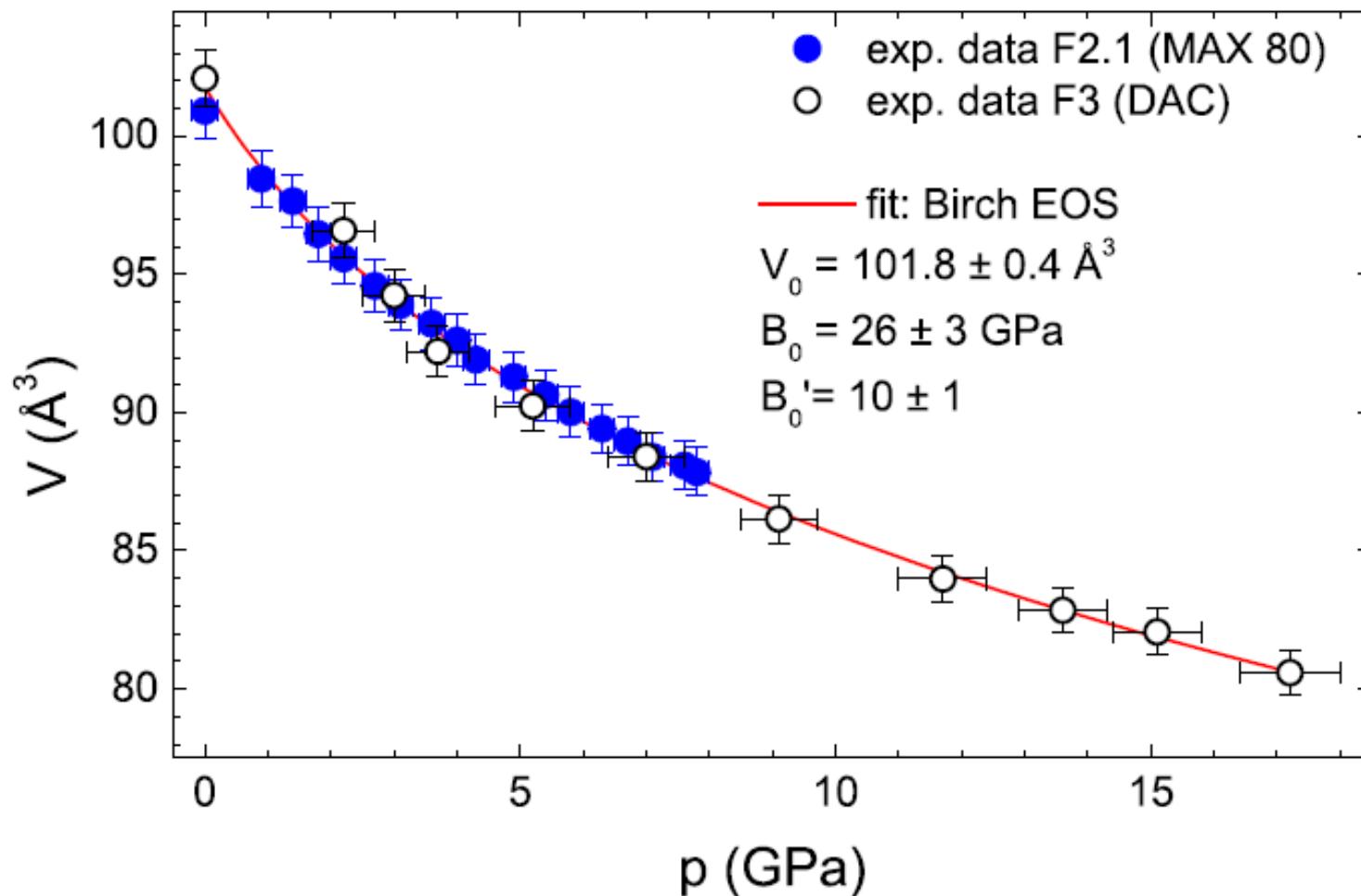
**What drives the pressure-induced electronic phase
transition ?**



**Structural instability due to layered structure under
pressure?**

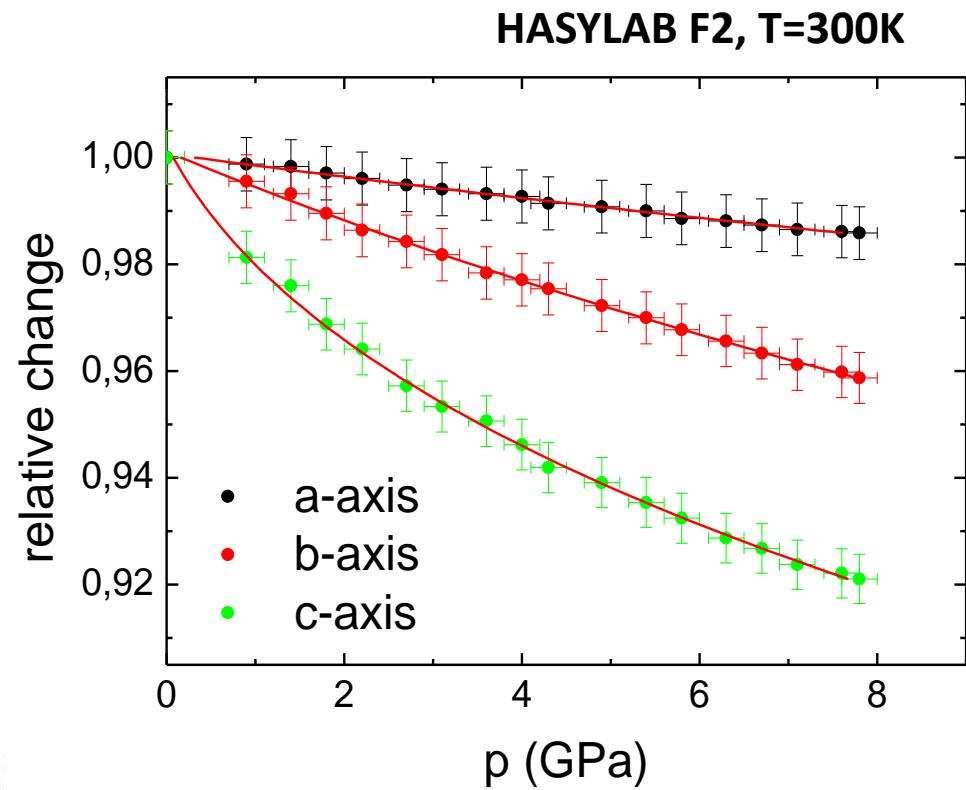
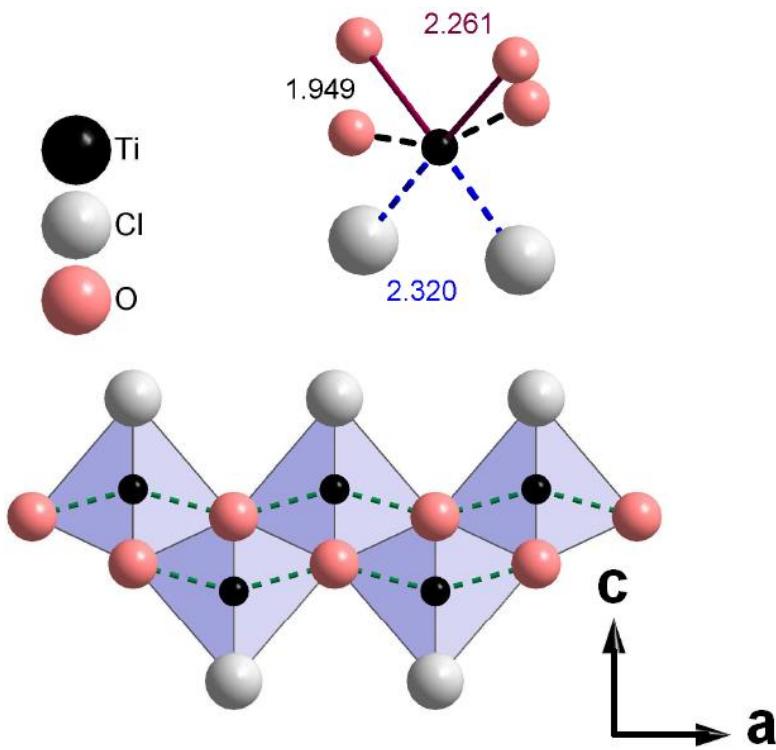
pressure dependence of the volume at room temperature

HASYLAB F2.1 (MAX 80) and F3 (DAC), T=300K, EDXRD



small Bulk modulus
no indication of a structural phase transition up to $\sim 17 \text{ GPa}$ within the experimental resolution

pressure dependence of a-, b- and c-axis at room temperature



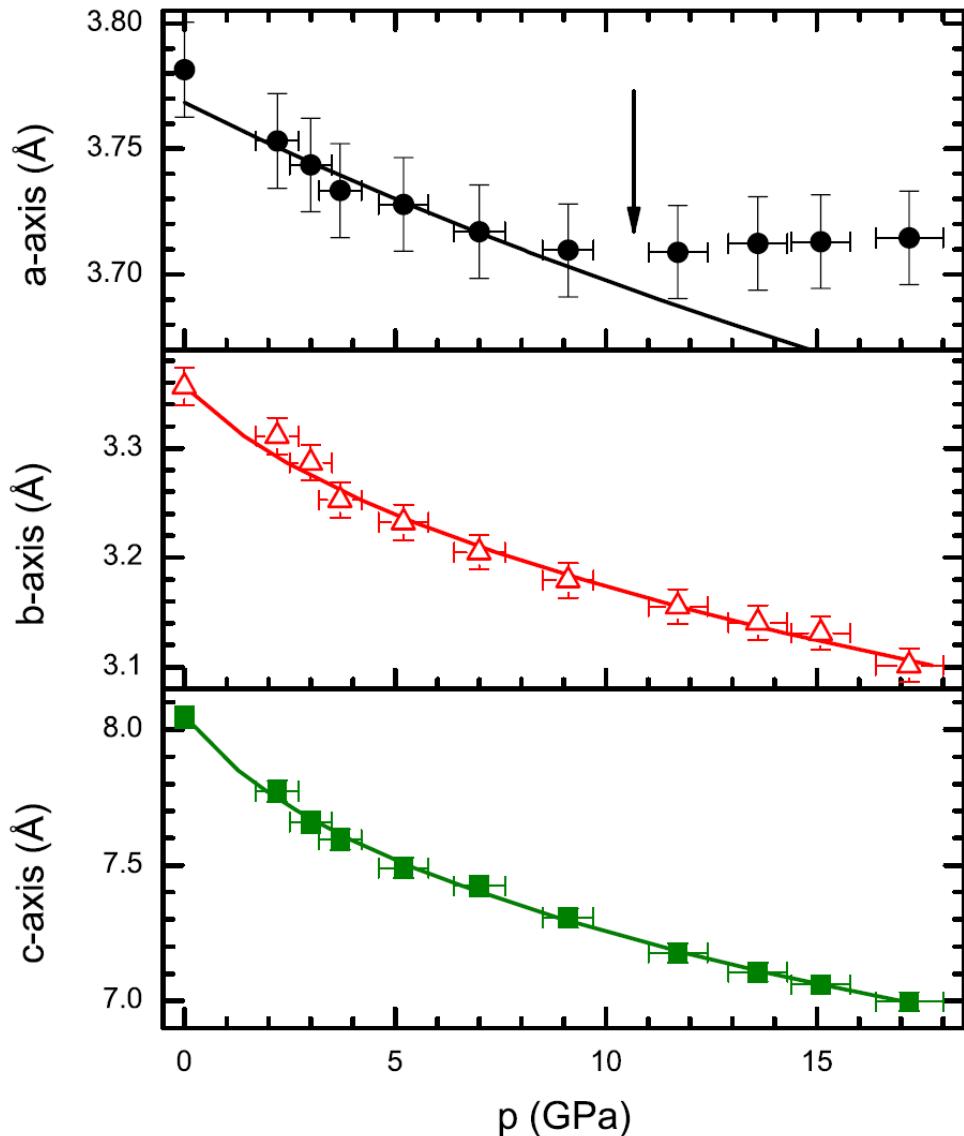
$B_a/B_c \approx 15 \Rightarrow$ extreme large anisotropy



structural instability - consequence:
Possibility of structural phase transition at higher pressure?
 \Rightarrow driving mechanism of electronic phase transition above 13 GPa?

pressure dependence of the lattice parameters at room temperature

connection between structure and electrical transport:



simple picture:
direct hopping (Ti-Ti) along b
indirect hopping (Ti-O-Ti) along a

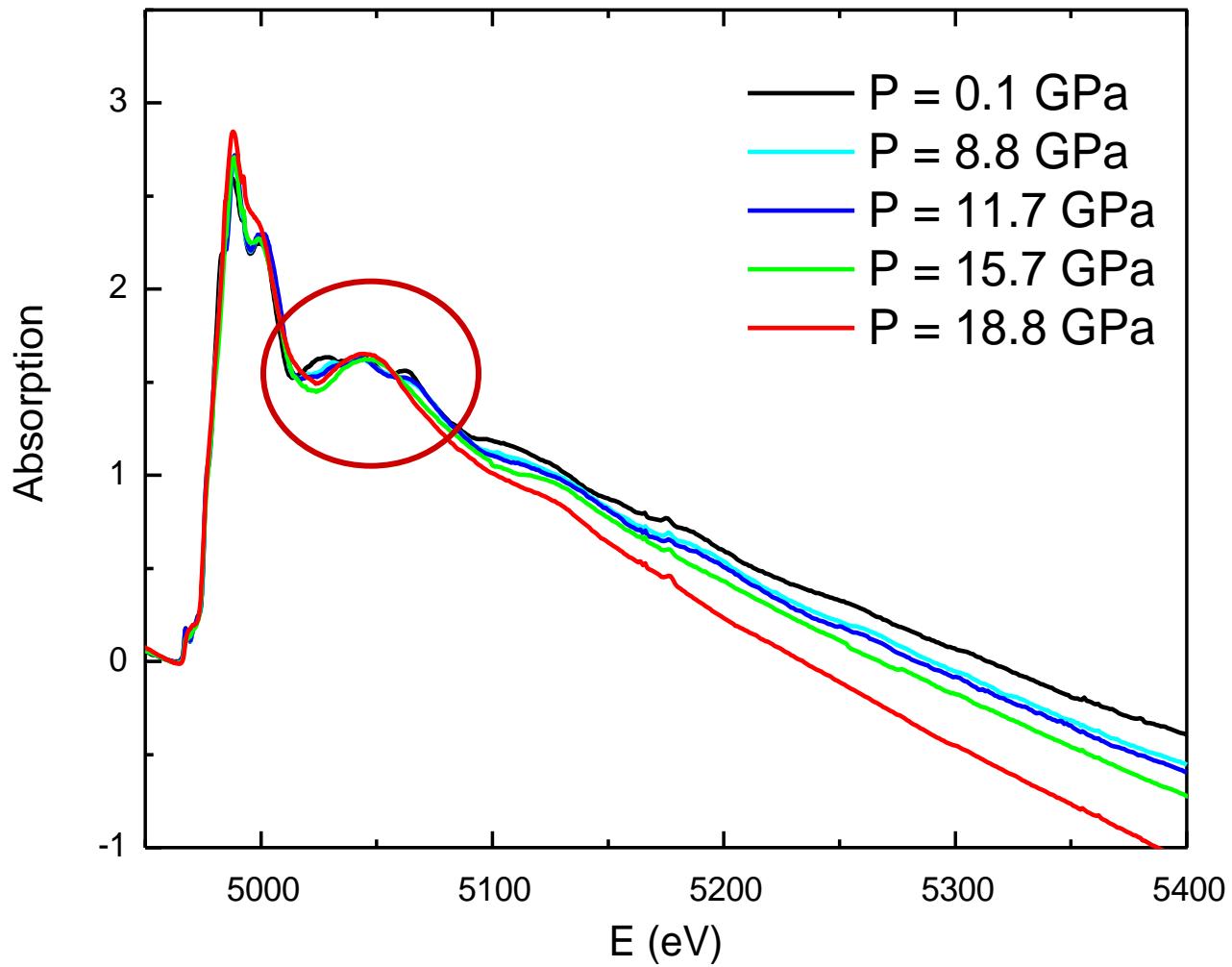
anomaly of the a -axis above 10 GPa strongly affects the indirect hopping (Ti-O-Ti) and transport along a
 \Rightarrow anomaly in $E_g(p)$!

Further structural studies required!

Extended X-ray Absorption Fine Structure (EXAFS)

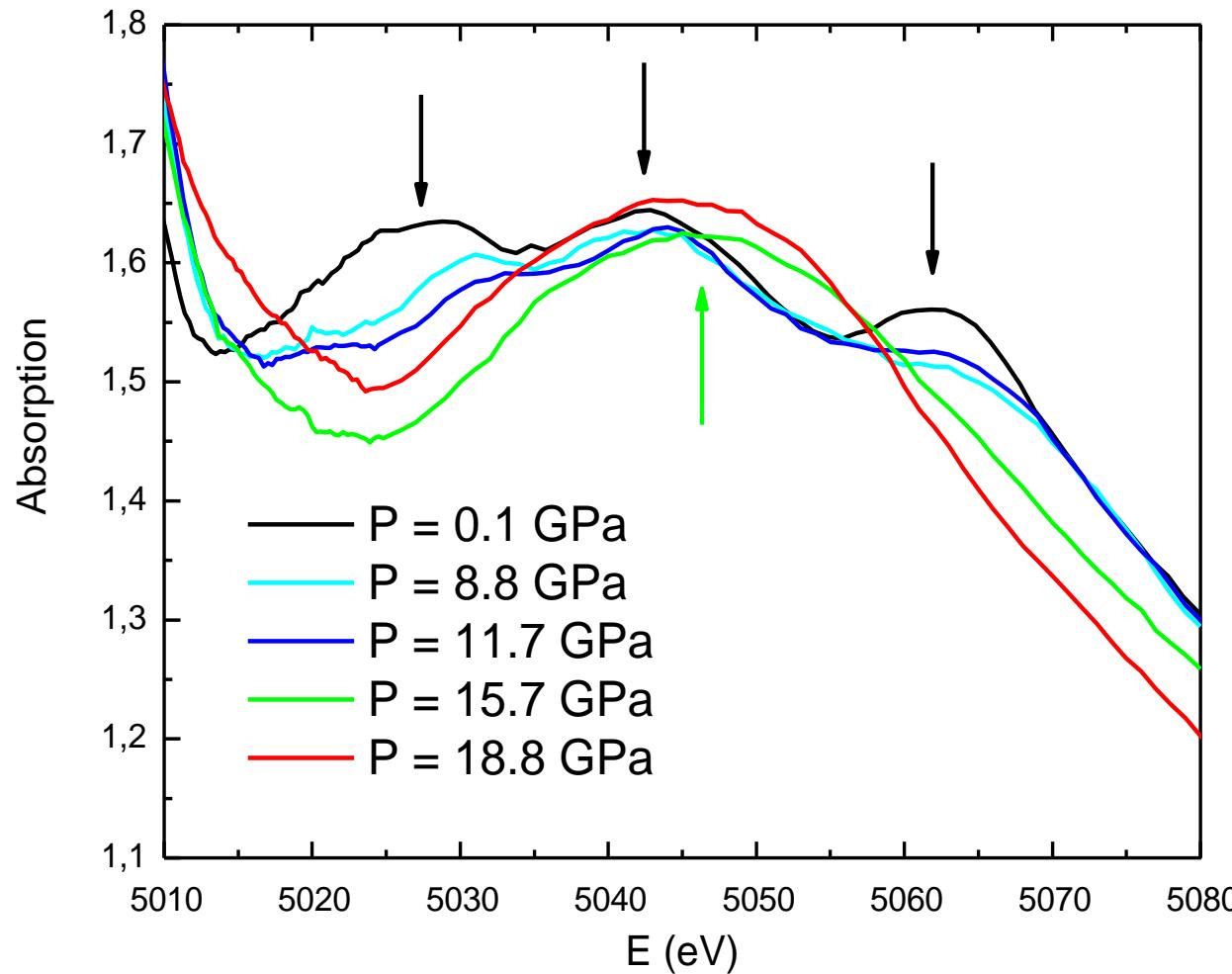
EXAFS
→ informations about:

- numbers and distances of next neighbors of Ti
- Ti-Ti distances



local structure under pressure probed by EXAFS (Ti K-Edge)

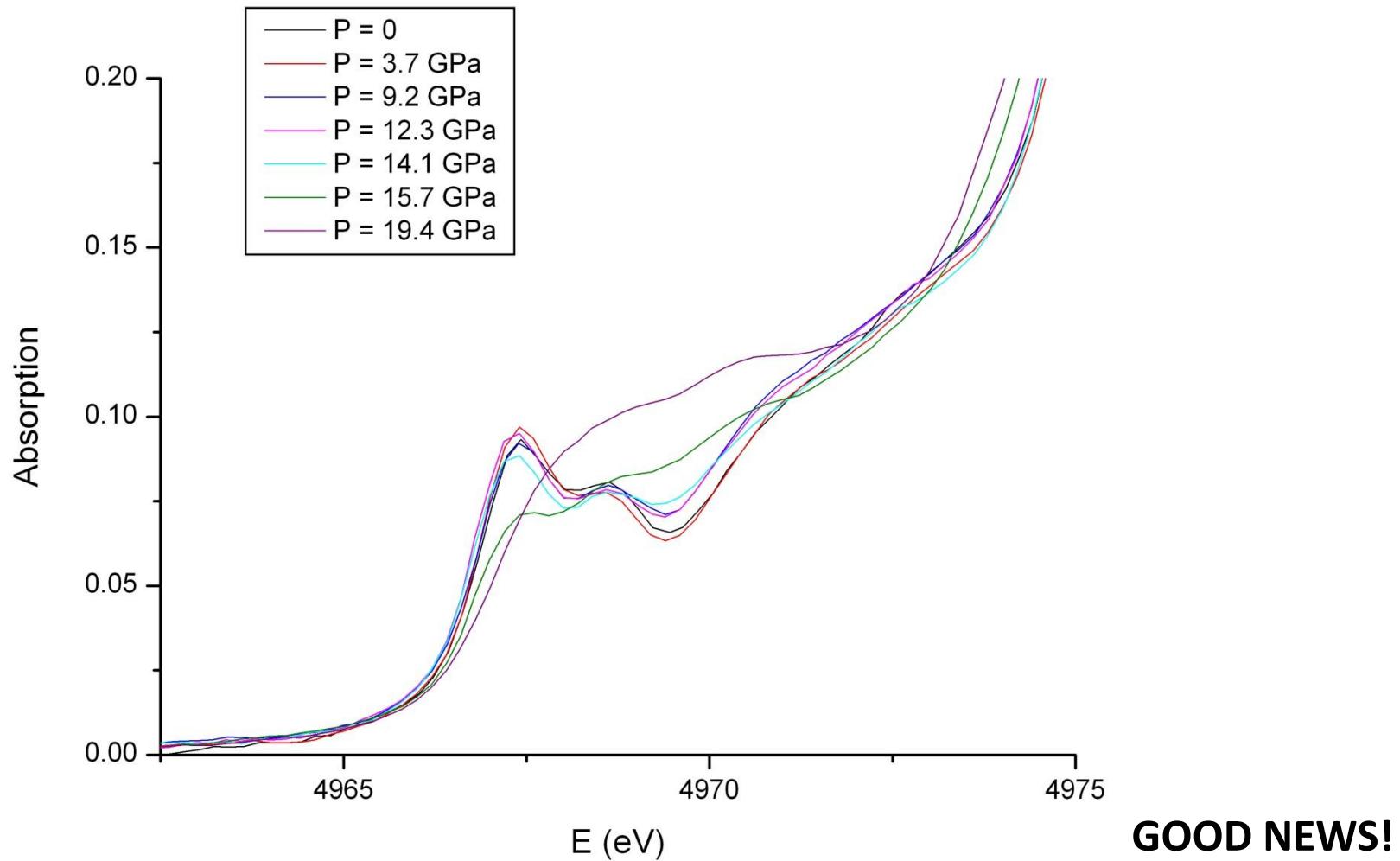
Extended X-ray Absorption Fine Structure (EXAFS)



GOOD NEWS!

Significant modification of EXAFS signal
⇒ change in local structure around Ti atoms above 12 GPa!

pre-edge (EXAFS)



GOOD NEWS!

Significant modification of the pre-edge part of EXAFS
⇒ change of electronic structure above 12 GPa!

Extended X-Ray Absorption Fine Structure (EXAFS)

bad news:

no quantitative analysis possible!

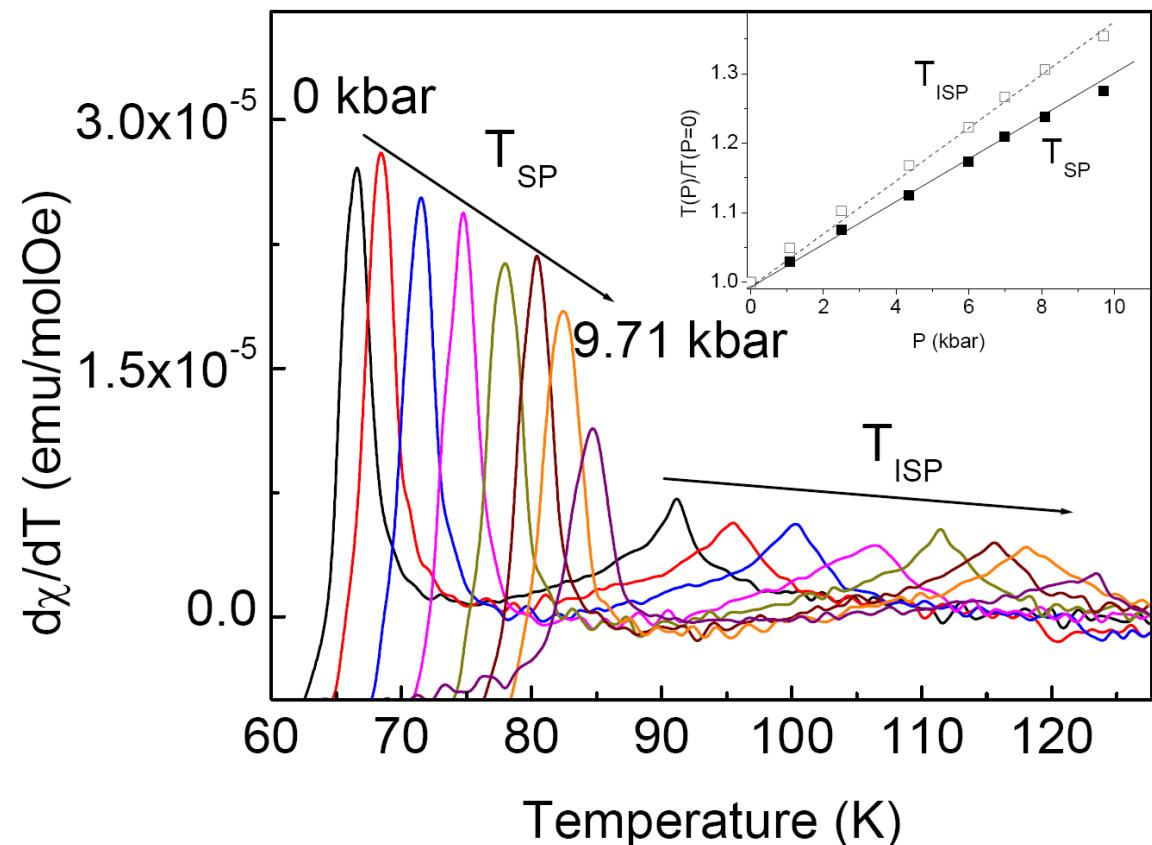
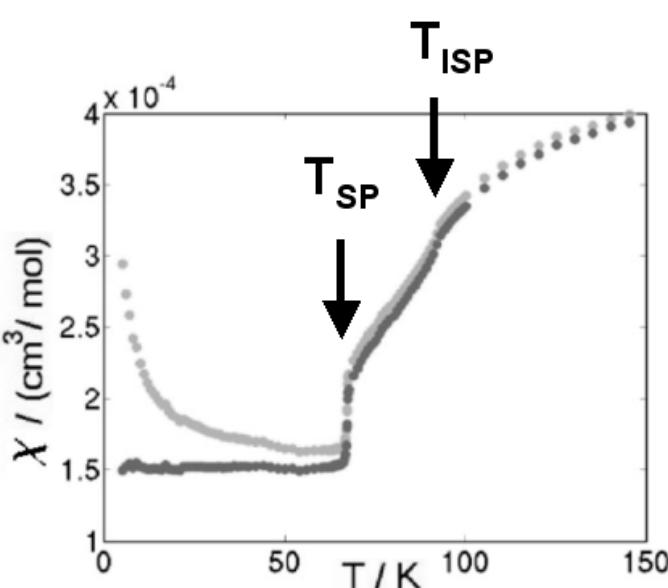
EXAFS signals: main problem → positional beam instability

- ⇒ different amplitudes of EXAFS wiggles
- ⇒ inaccurate analysis

pre-edge structure:

analysis requires solid work on ab-initio calculations

pressure dependence of spin-Peierls transition T_{SP}

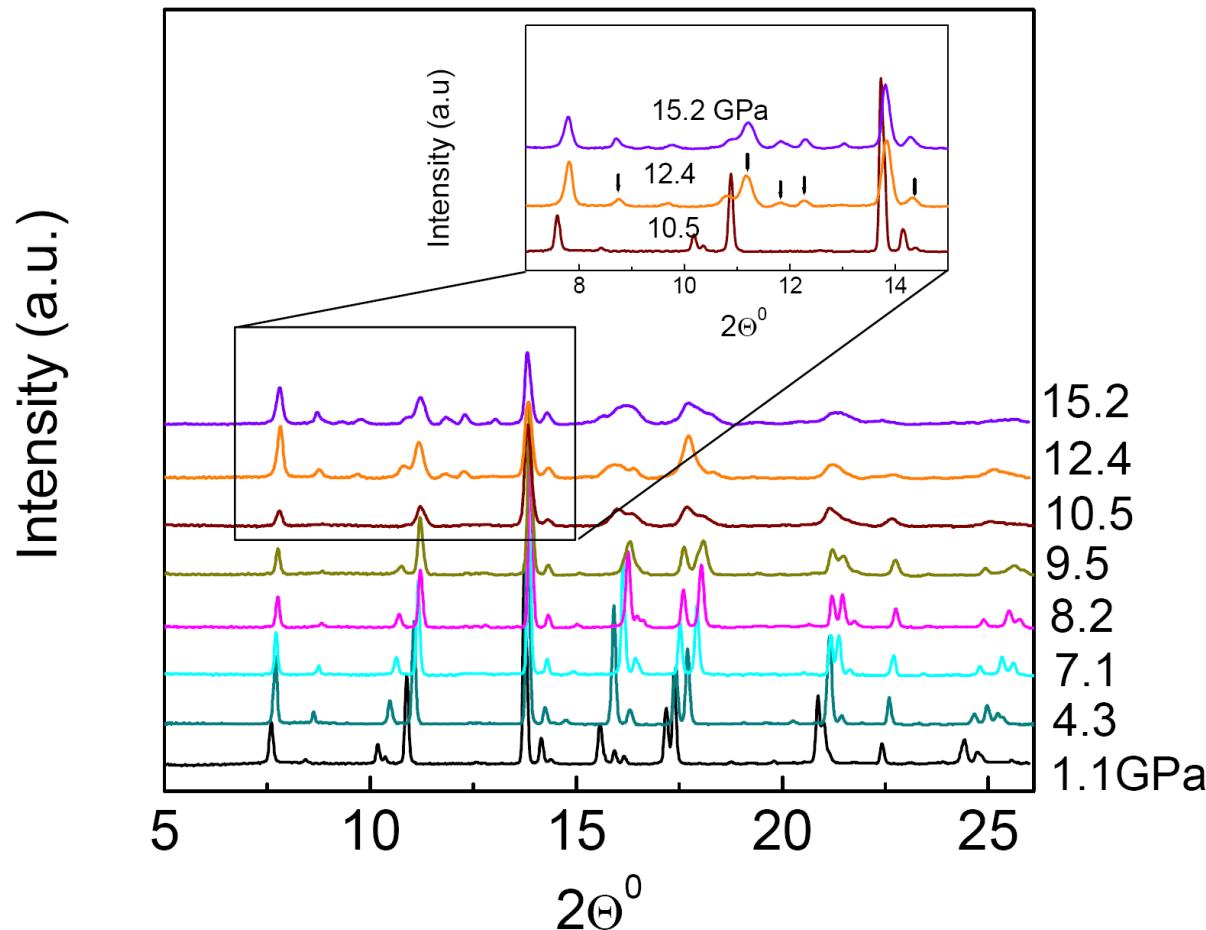


$\text{TiOCl}: \partial \ln T_{SP} / \partial p = 2.88 \cdot 10^{-1} \text{GPa}^{-1}, \partial \ln T_{ISP} / \partial p = 3.64 \cdot 10^{-1} \text{GPa}^{-1}$
 $(\text{TiOBr}: \partial \ln T_{SP} / \partial p = 3.4 \cdot 10^{-1} \text{GPa}^{-1}, \text{Fausti et al., PRB (2007)})$

T_{SP} strongly increases with pressure
 \Rightarrow consistent with enhanced dimerization at 300 K!

angle dispersive x-ray diffraction

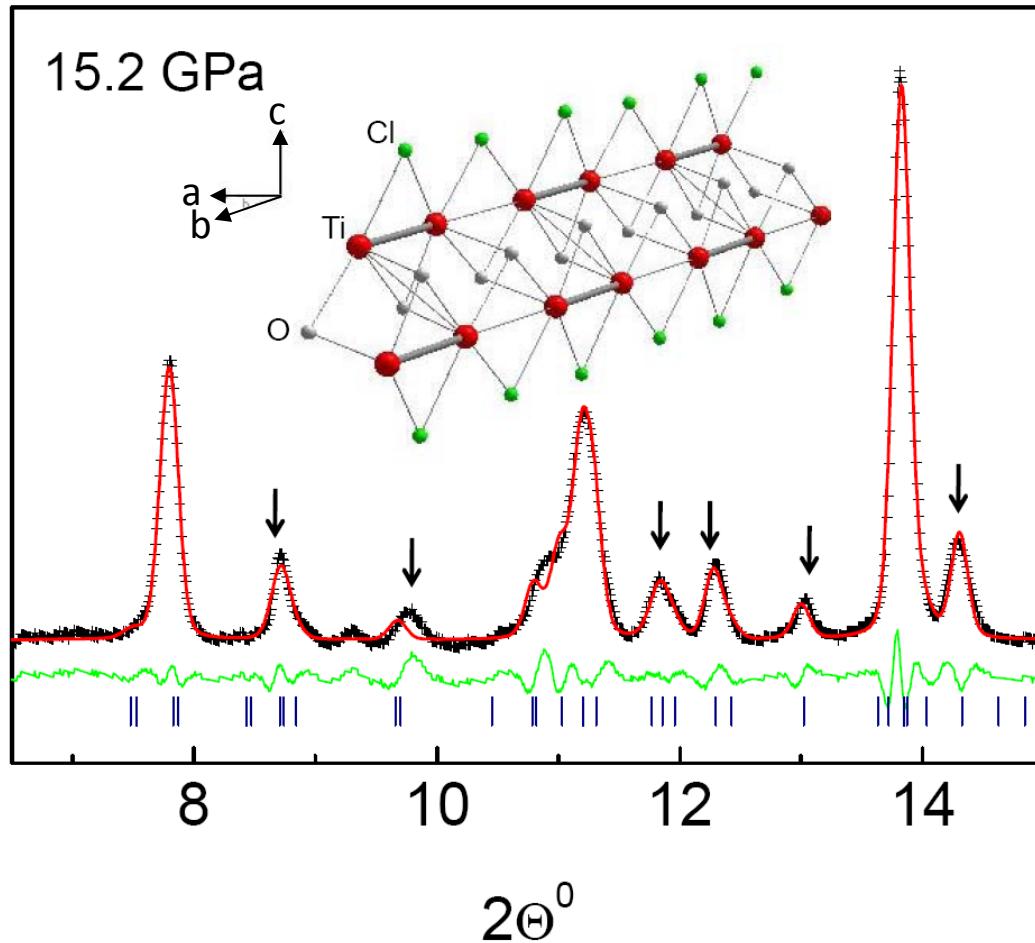
Daresbury Synchrotron Radiation Source (Warrington, UK)



pressure-induced structural phase transition above 11 GPa!

Rietveld refinement: structural phase transition (orthorhombic $Pmmn$ → monoclinic $P2_1/m$)

Intensity (a.u.)



Two inequivalent Ti^{3+} sites along the *b* direction in monoclinic $P2_1/m$:

Ti-Ti (short): 2.95 Å
Ti-Ti (long): 3.69 Å
→ $\Delta d \sim 20\%$

(ambient pressure: $\Delta d \sim 5\%$ at low T)

⇒ enhanced dimerization under pressure at 300 K!

Theoretical description of structural and electronic properties of TiOCl under high pressure

Victor Pardo

Ab initio studies at high pressure on TiOCl: electronic structure of the orthorhombic and monoclinic phases

Gap evolution

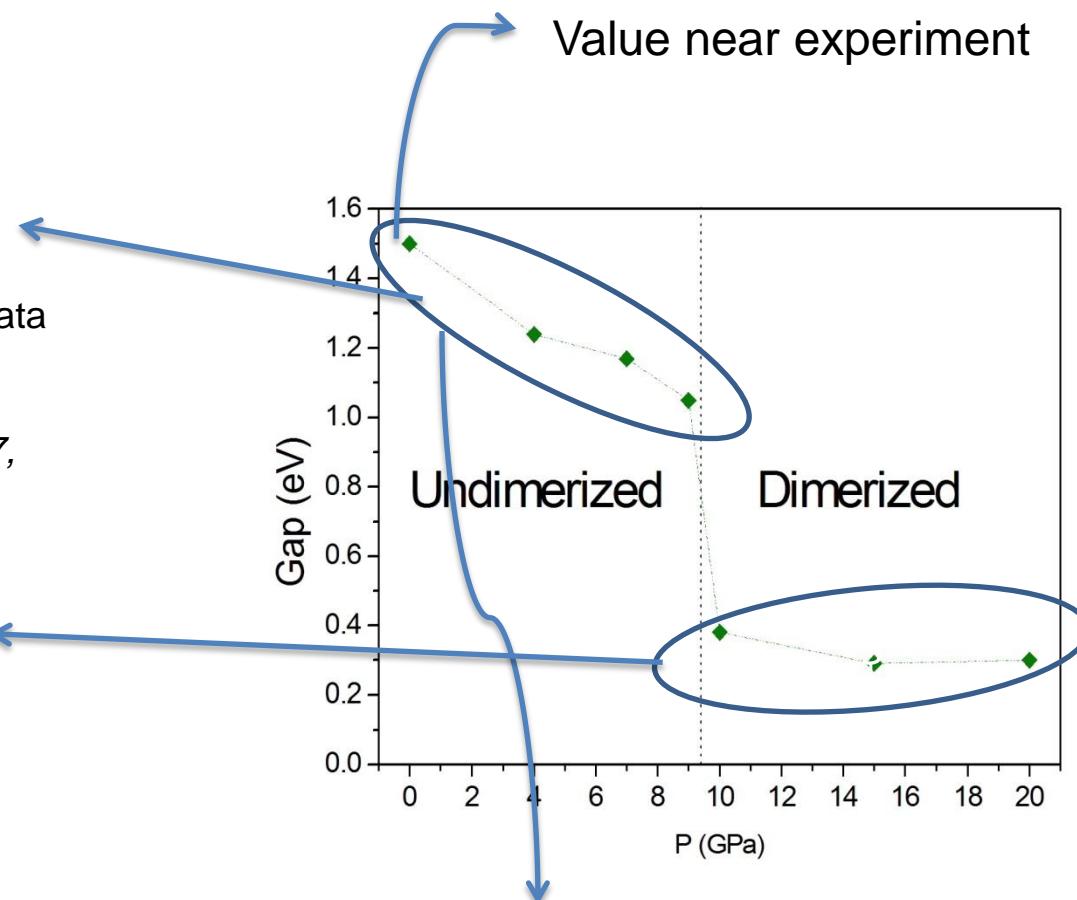
Decrease of the gap ~ 30%
In orthorhombic structure

In concordance with experimental data
(resistivity measurements):

M.K. Forthaus et al., Phys. Rev. B 77,
165121 (2008)

Drastic reduction of the gap:
Structural transition

In concordance with experiment



We would need more than 30 GPa to get an insulator-to-metal transition in orthorhombic structure!!

Ab initio studies at high pressure on TiOCl: electronic structure of the orthorhombic and monoclinic phases

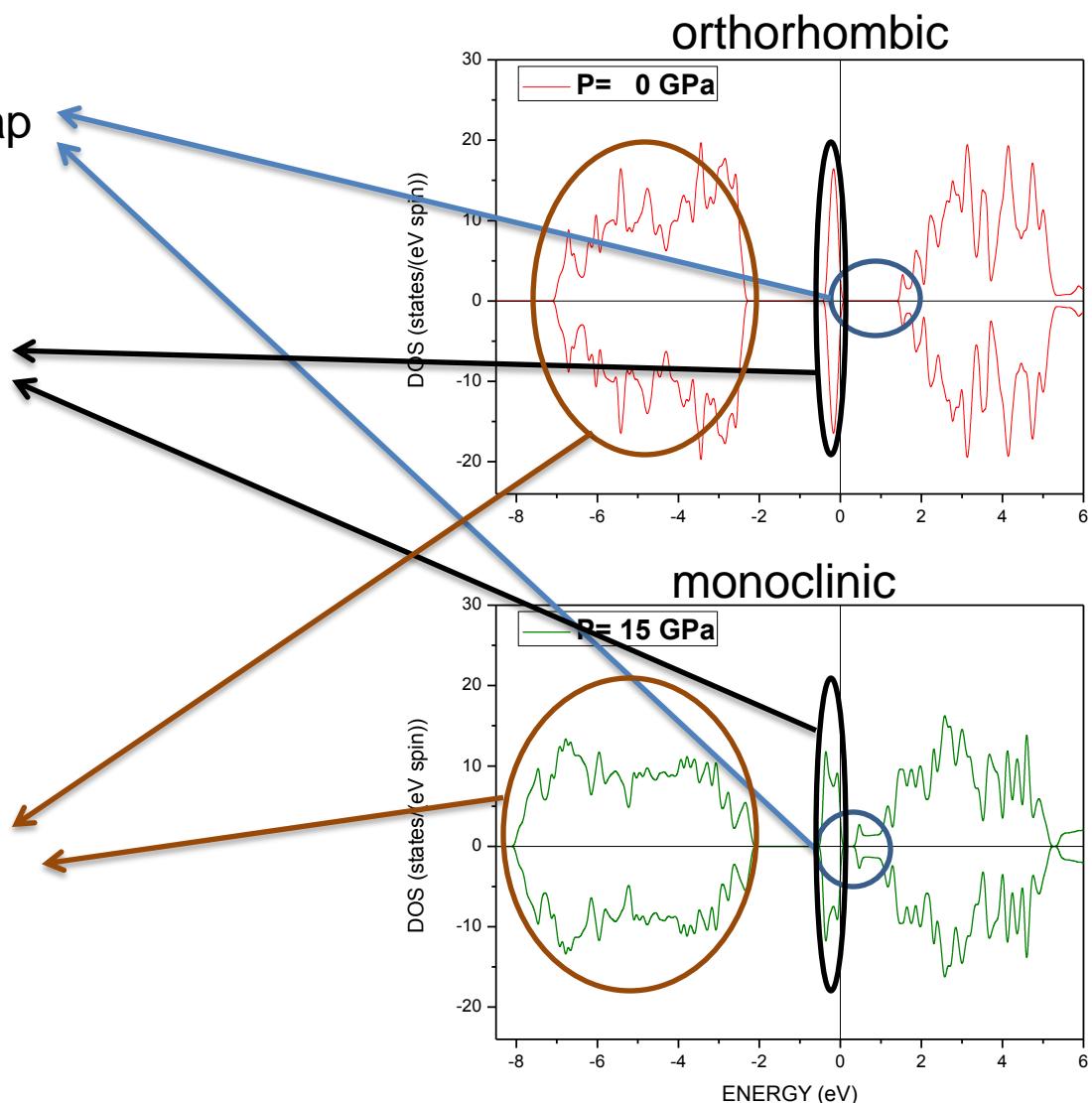
Drastic reduction of the gap
(from 1.5 eV to 0.3 eV)

States of d¹ electron of Ti are
good localized in a ~ 1 eV
band near Fermi energy

Mot-Hubbard type gap (d-d
gap)

Increase ~20% of the
bandwidth

Oxygen bands are in
energies down than -2 eV

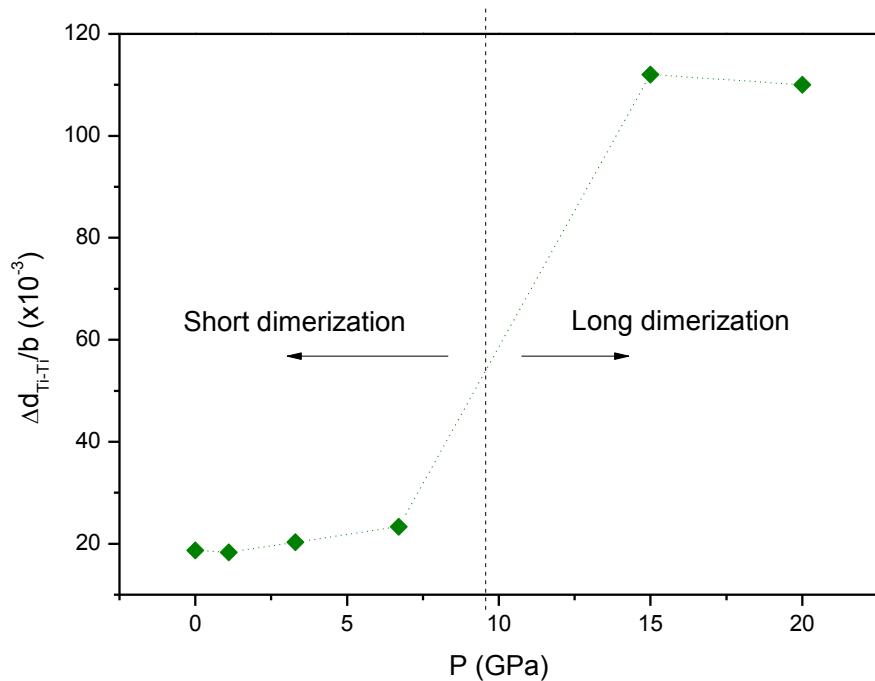
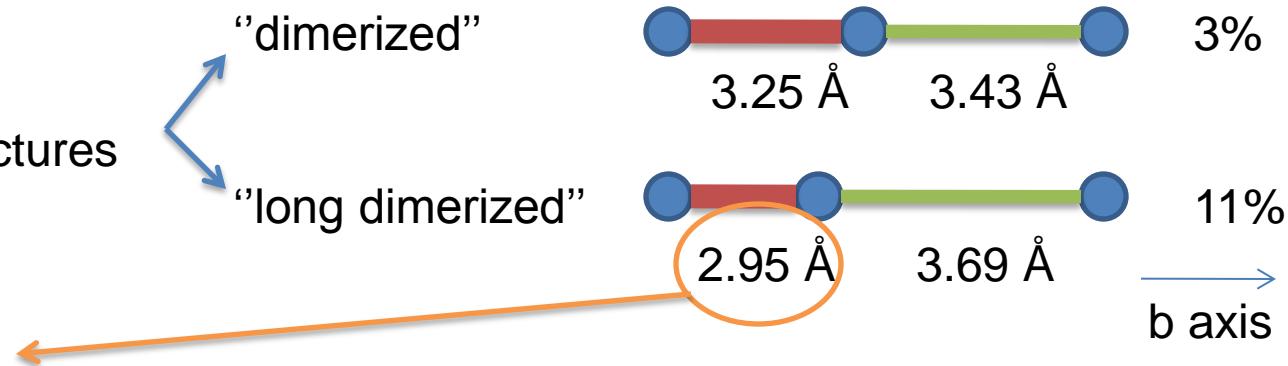


Ab initio studies at high pressure on TiOCl: electronic structure of the orthorhombic and monoclinic phases

Monoclinic space group:
2 types of dimerized structures

● Ti atom

Close to metal Ti bond length!!!
Limit for electron-itinerancy
Spin-Peierls distortion is expected to be supported by a conventional Peierls distortion of the 1D chain



Strongly correlated transition metal systems

Recent high pressure studies:

→ **TiOCl: low dimensional spin 1/2 system (Ti^{3+} ; $3d^1$) Mott insulator**

**Metal Cluster compounds: AM_4X_8 ($A=Ga$; $M=Nb, Ta$; $X=S, Se$)
a new class of Mott insulators**

superconductivity close to a Mott transition

conventional superconductivity

H		ambient pressure superconductor								high pressure superconductor								He
Li	Be 0.026 14 30				T _c (K) T _c ^{max} (K) P(GPa)					T _c ^{max} (K) P(GPa)								
Na	Mg																	
K	Ca 15 150	Sc 0.35 21	Ti 0.39 5.38 16.5 120	V 5.38 16.5 120	Cr	Mn	Fe 2.1 21	Co	Ni	Cu	Zn 0.875	Ga 1.091 7 1.4	Ge	As	Se	Br 1.4 100	Kr	
Rb	Sr 7 50	Y 19.5 115	Zr 0.546 11 30	Nb 9.50 9.9 10	Mo 0.92	Tc 7.77	Ru 0.51	Rh .00033	Pd	Ag	Cd 0.56	In 3.404	Sn 3.722 5.3 11.3	Sb	Te	I 1.2 25	Xe	
Cs	Ba 1.3 12	insert La-Lu 5 18	Hf 0.12 8.6 62	Ta 4.483 4.5 43	W 0.012	Re 1.4	Os 0.655	Ir 0.14	Pt	Au	Hg- α 4.153	Tl 2.39	Pb 7.193	Bi 8.5 9.1	Po	At	Rn	
Fr	Ra	insert Ac-Lr	Rf	Ha														

La-fcc 6.00 13 15	Ce 1.7 5	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu 2.5 22
Ac	Th 1.368	Pa 1.4	U 0.8(β) 2.4(α) 1.2	Np	Pu	Am 0.79 2.2 6	Cm	Bk	Cf	Es	Fm	Md	No	Lr

conventional superconductivity ?

H		ambient pressure superconductor										high pressure superconductor										He					
Li	Be 0.026																					Ne					
14																											
30																											
Na	Mg																					Al 1.14	Si	P	S	Cl	Ar
K	Ca	Sc	Ti 0.39	V 5.38	Cr	Mn	Fe 2.1	Co 21	Ni	Cu	Zn 0.875	Ga 1.091	Ge	As	Se	Br	Kr										
	15	0.35	21	16.5	120						7	1.4	5.35	2.4	8	1.4											
	150										11.5	32	150	100													
Rb	Sr	Y	Zr 0.546	Nb 9.50	Mo 0.92	Tc 7.77	Ru 0.51	Rh .00033	Pd	Ag	Cd 0.56	In 3.404	Sn 3.722	Sb	Te	I	Xe										
	7	19.5	11	9.9	10						5.3	11.3	3.9	7.5	1.2												
	50	115	30								25	35	25	35	25												
Cs	Ba	insert La-Lu	Hf 0.12	Ta 4.483	W 0.012	Re 1.4	Os 0.655	Ir 0.14	Pt	Au	Hg- α 4.153	Tl 2.39	Pb 7.193	Bi	Po	At	Rn										
	1.3	5	8.6	4.5	62	43																					
	12	18																									
Fr	Ra	insert Ac-Lr	Rf	Ha																							

La-fcc 6.00	Ce 1.7	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu 2.5	22
	13 15														
Ac	Th 1.368	Pa 1.4	U 0.8(β) 2.4(α) 1.2	Np	Pu	Am 0.79 2.2 6	Cm	Bk	Cf	Es	Fm	Md	No	Lr	

Motivation:

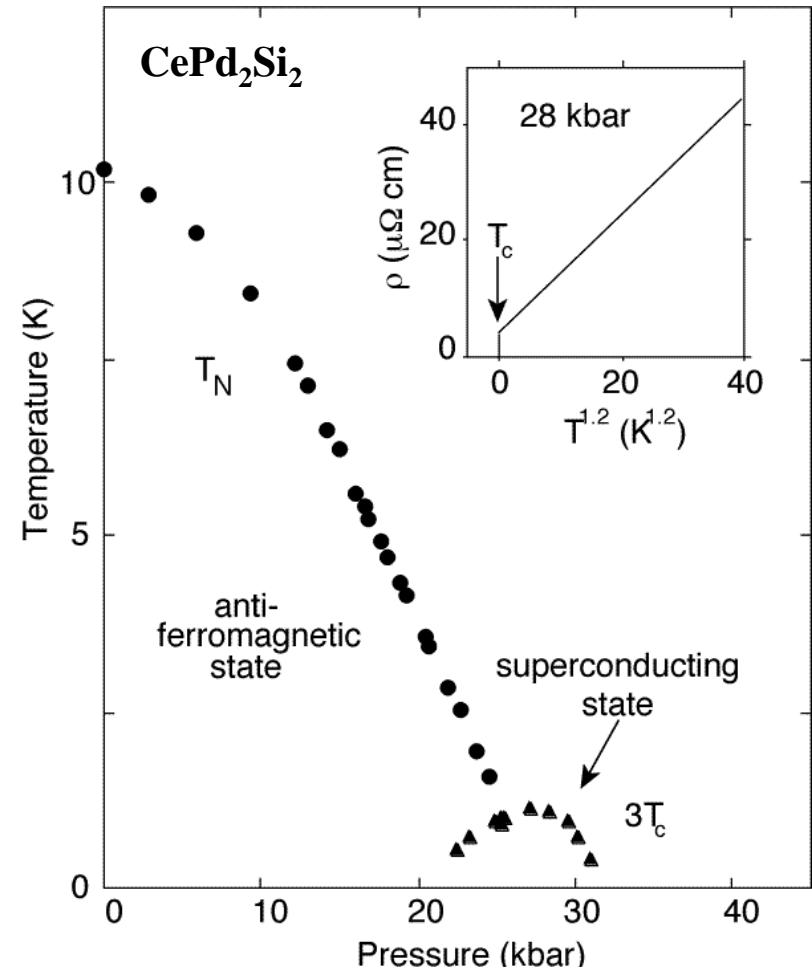
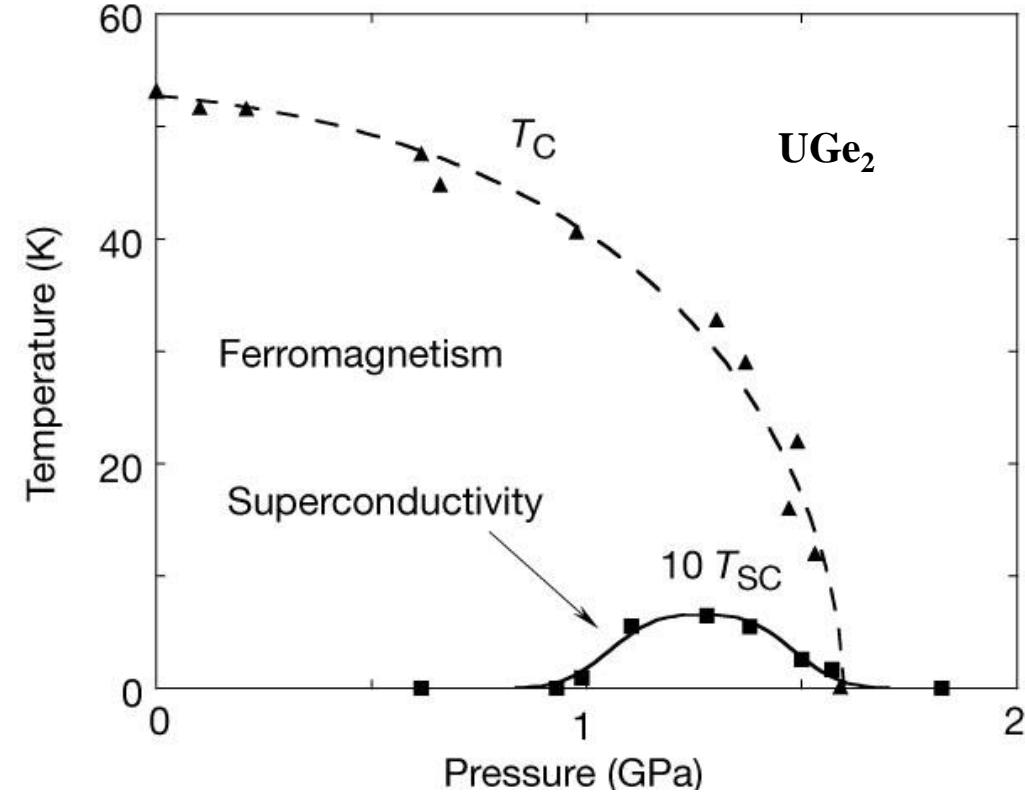
Search for superconductivity in the presence of
strong electron correlations.



different concepts!

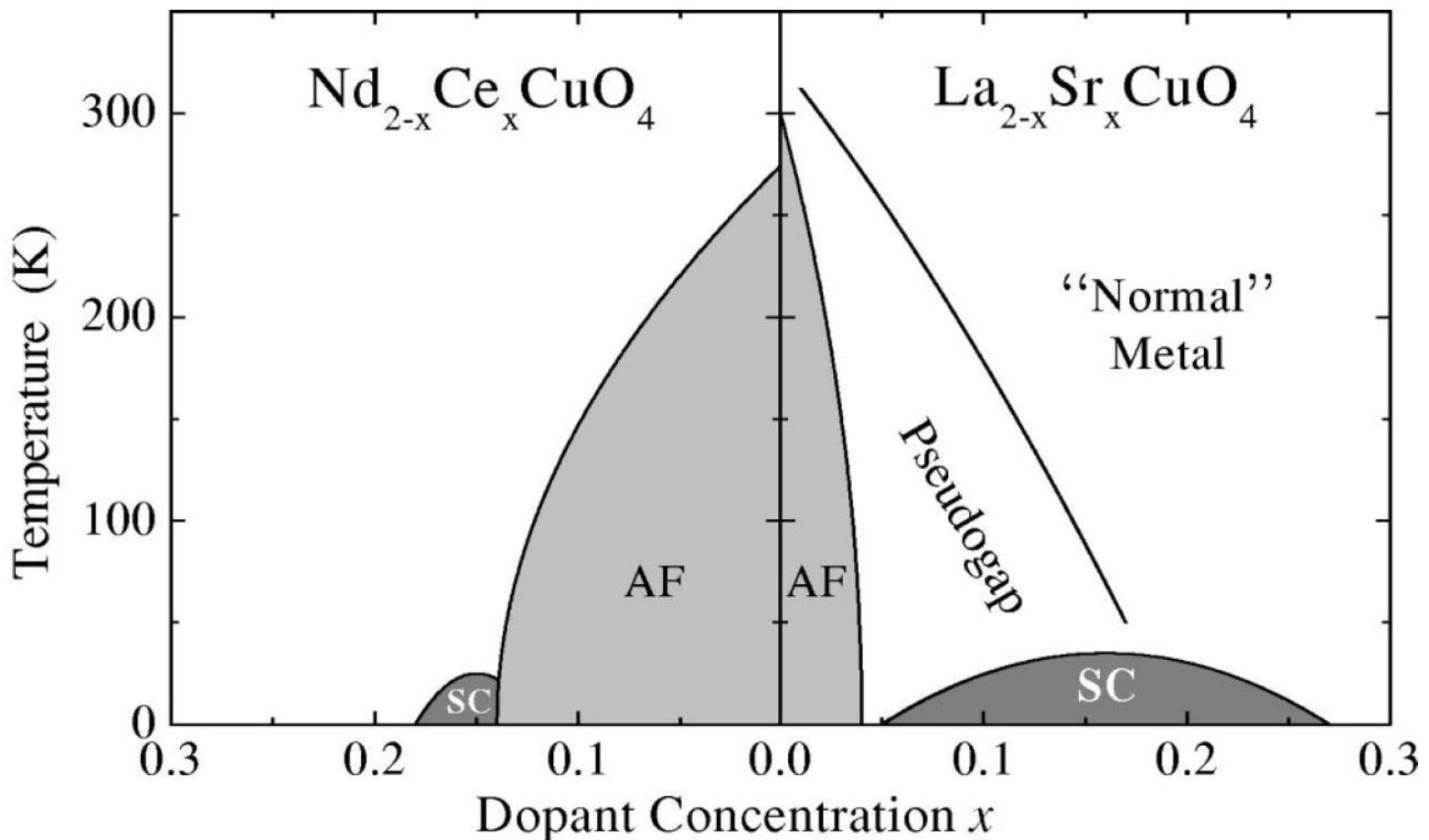
a) Metallic systems on the border of itinerant electron magnetism

Heavy fermion systems



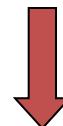
b) doped Mott-Insulators

HTC-Superconductors



c) stoichiometric Mott-Insulators

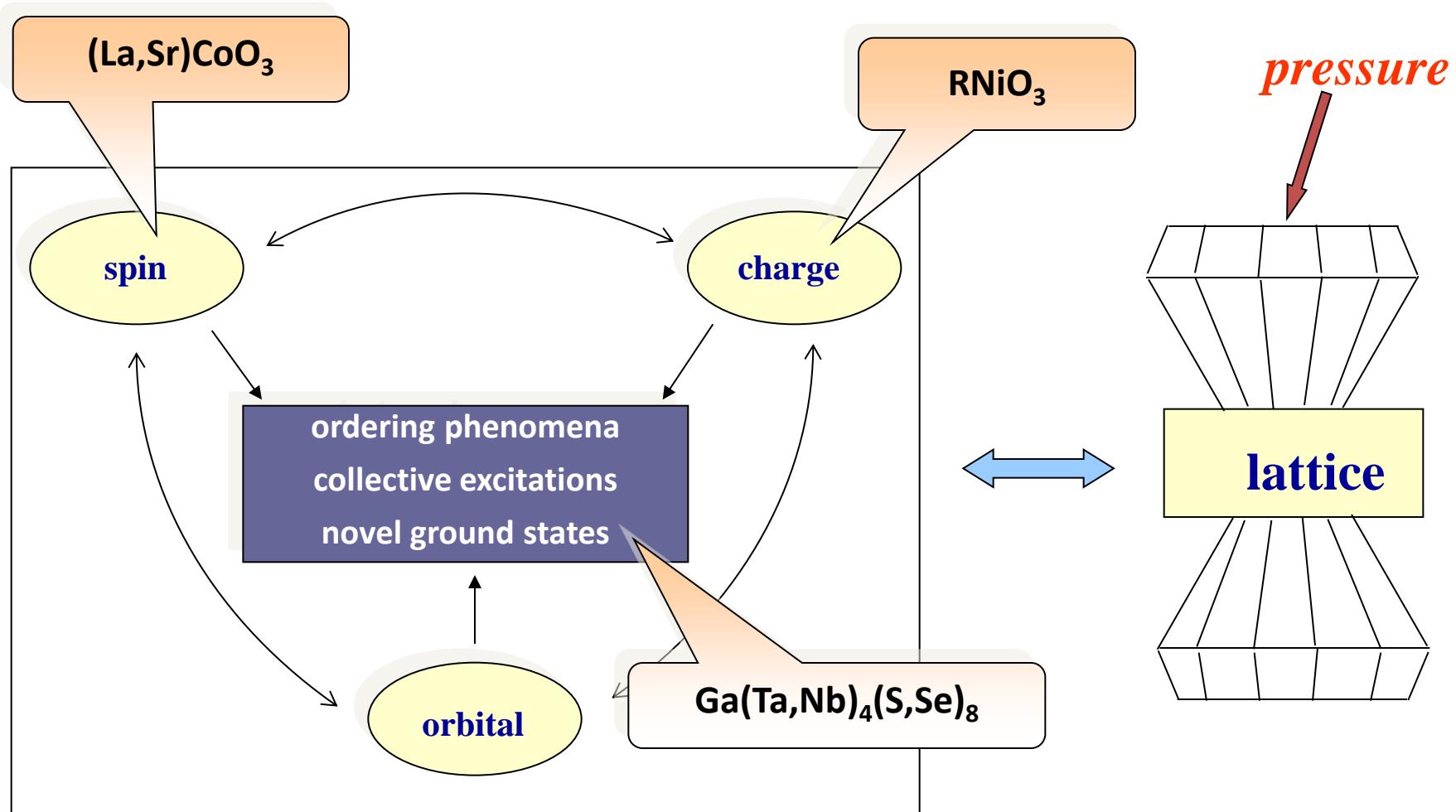
Another option



inducing superconductivity by pressure in
stoichiometric systems in the proximity to a Mott
transition

Advantage → Absence of disorder!

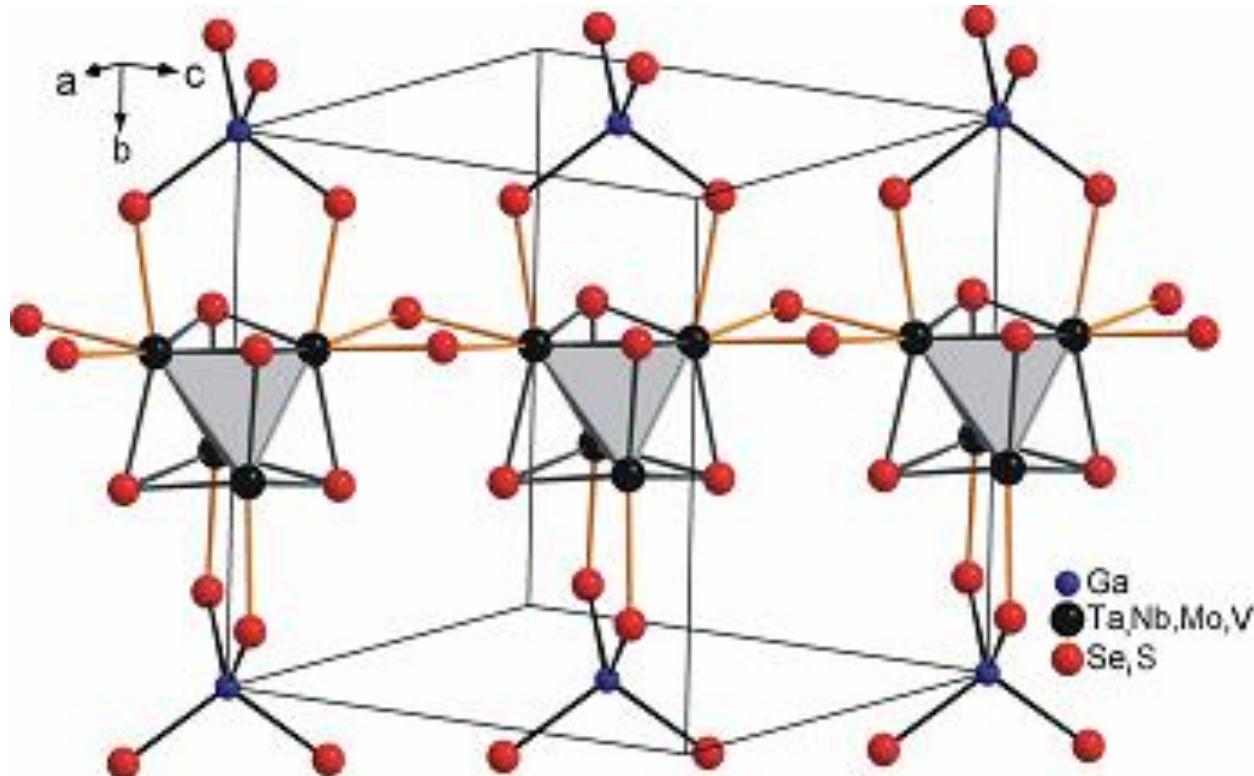
Selected correlated oxides



Metal-Insulator transition is driven by interplay between the degrees of freedom \Rightarrow anomalous metallic state

Metal Cluster compounds: AM_4X_8 ($A=Ga, Ge$; $M=V, Mo, Nb, Ta$; $X=S, Se$)

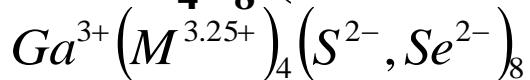
$GaMo_4S_8$ (fcc structure)



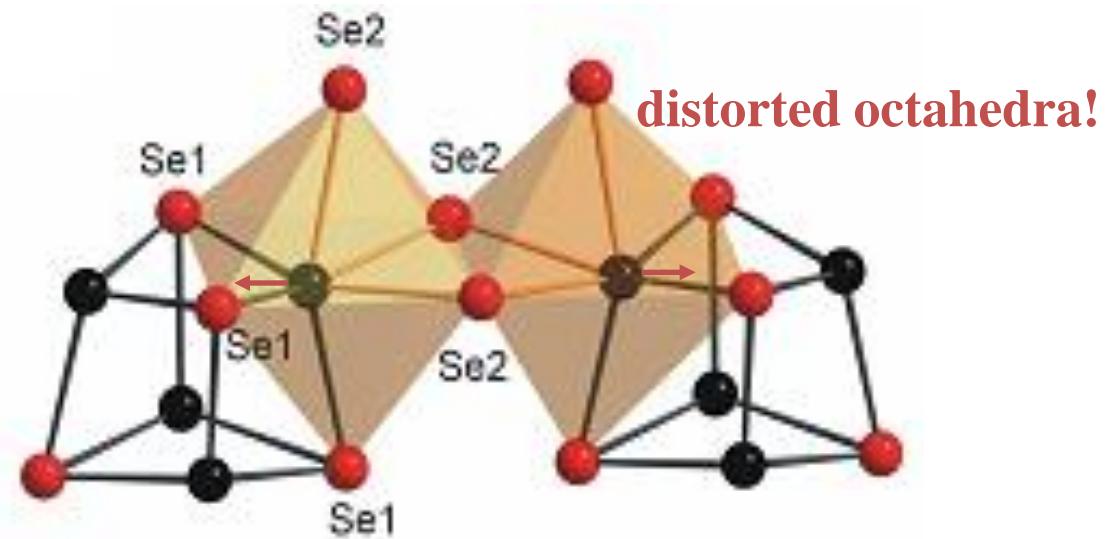
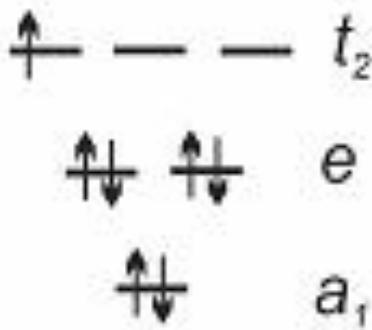
Tetrahedral M_4X_4 -metal clusters separated by large distances $\approx 4 \text{ \AA}$ and weakly coupled through S, Se anions. \Rightarrow localization of electronic states in the clusters

Metal Cluster compounds: AM_4X_8 ($A=Ga,Ge$; $M=V,Mo,Nb,Ta$; $X=S,Se$)

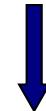
$GaMo_4S_8$ (fcc structure)



Mott-Insulators: with $S = 1/2$
(Ga^{3+})



Ground state properties strongly depend on the local structure of the M_4 -cluster; mainly on the number of valence electrons per cluster.



Consequences?

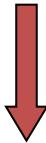
Consequences: localization of the electronic states in the clusters



- (a) non of these compounds show metallic conductivity, instead the electronic conduction takes place by hopping of carriers among the clusters.
⇒ semiconducting systems with a small energy gap (~ 0.1 eV);



- (b) Magnetic suseptibility is typical for localized spins (e.g. GaV_4Se_8 and GaV_4S_8 R. Pocha et al., Chem. Mater. (2000)).



Mott Insulators in which the „correlated units“ are M_4 -metal clusters!!
with extra internal degree of freedom?

Aim: Search for superconductivity under high pressure in the proximity to a Mott transition.

Systems and experimental methods:

Mott Insulators $\text{GaNb}_4(\text{S},\text{Se})_8$ and GaTa_4Se_8

- 1. Electrical resistance under high pressure up to 30 GPa and in external magnetic field up to 10 T using the Diamond Anvil Cell technique.**
- 2. Energy-Dispersive x-ray diffraction up to 30 GPa (Hasylab).**
- 3. Angle resolved x-ray diffraction on single crystal of GaTa_4Se_8 up to 15 GPa.**
- 4. Raman spectroscopy up to 20 GPa**

Results at ambient pressure

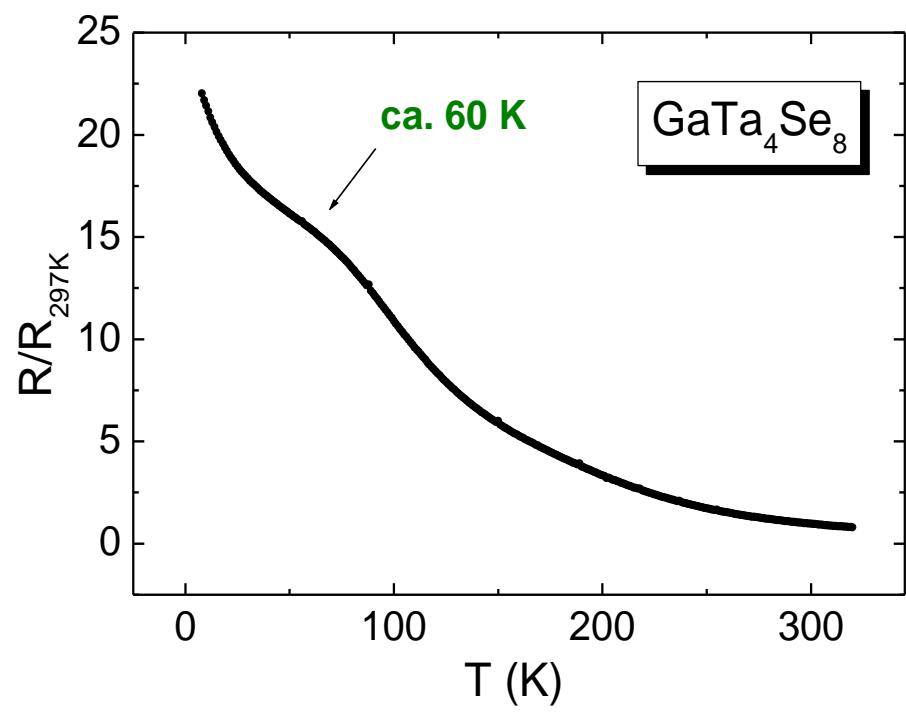
x-ray diffraction @300 K:

	a (Å)	V (Å ³)	d_{mm} (Å)	d_{cc} (Å)
GaNb₄Se₈	10.420(1)	1131.37	3.026(1)	4.320(1)
GaTa₄Se₈	10.358(2)	1111.29	3.002(2)	4.322(1)
GaNb₄S₈	9.985(2)	995.51	2.975(1)	4.085(1)

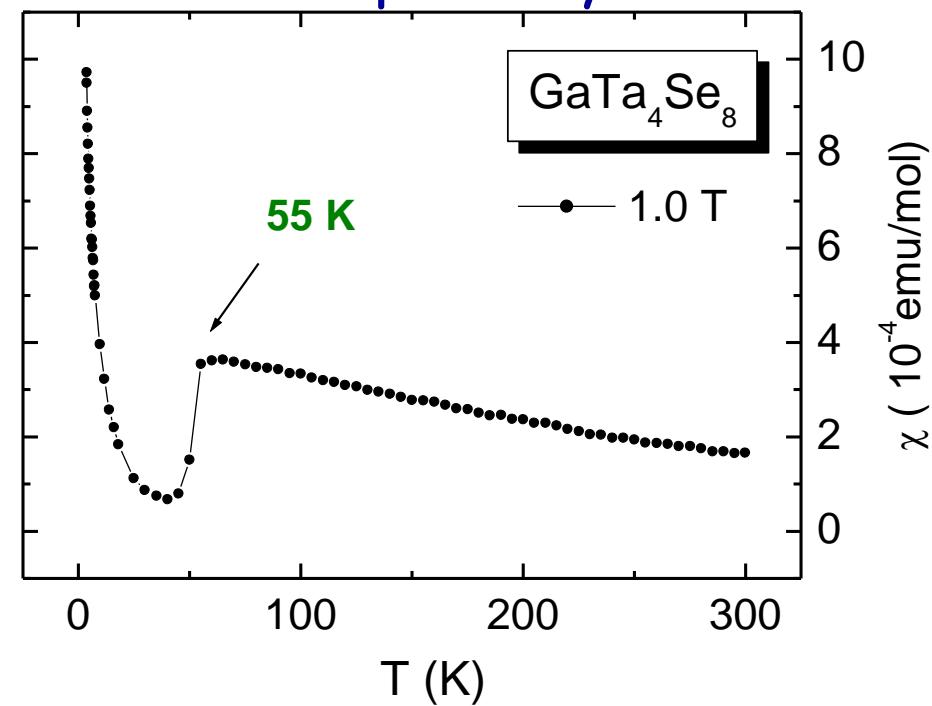
$$d_{cc} \gg d_{mm}$$

Results at ambient pressure:

Electrical resistance



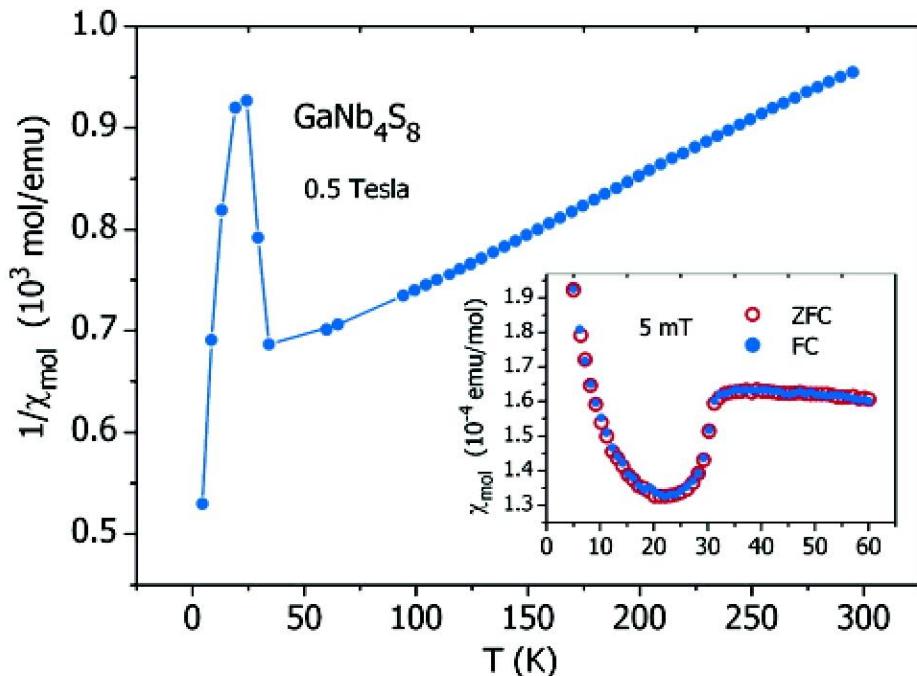
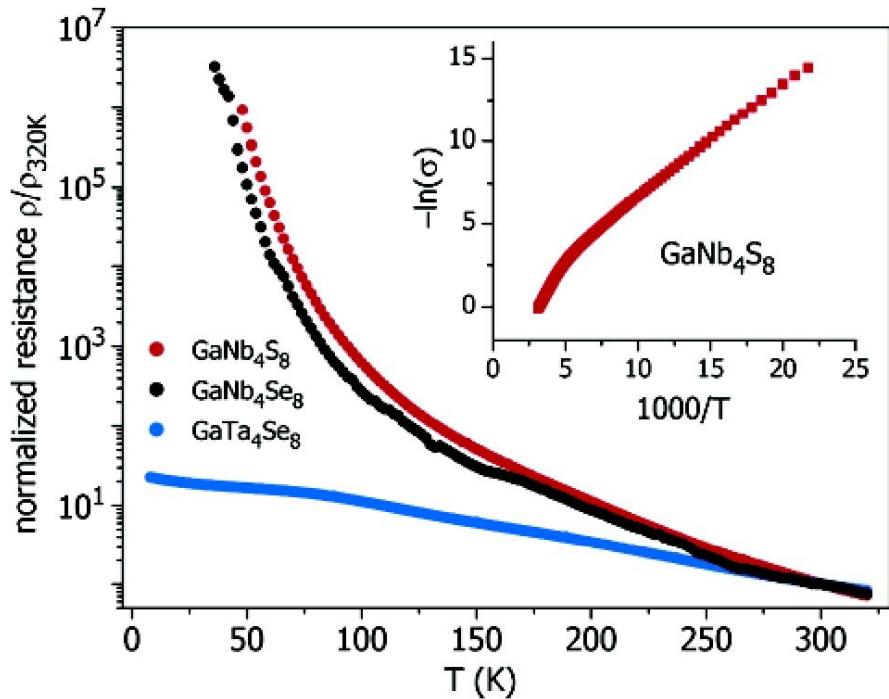
Magnetic susceptibility



$R(T) \Rightarrow$ small energy gap ~ 0.1 eV

$\chi(T) \Rightarrow$ sharp anomaly at low temperatures

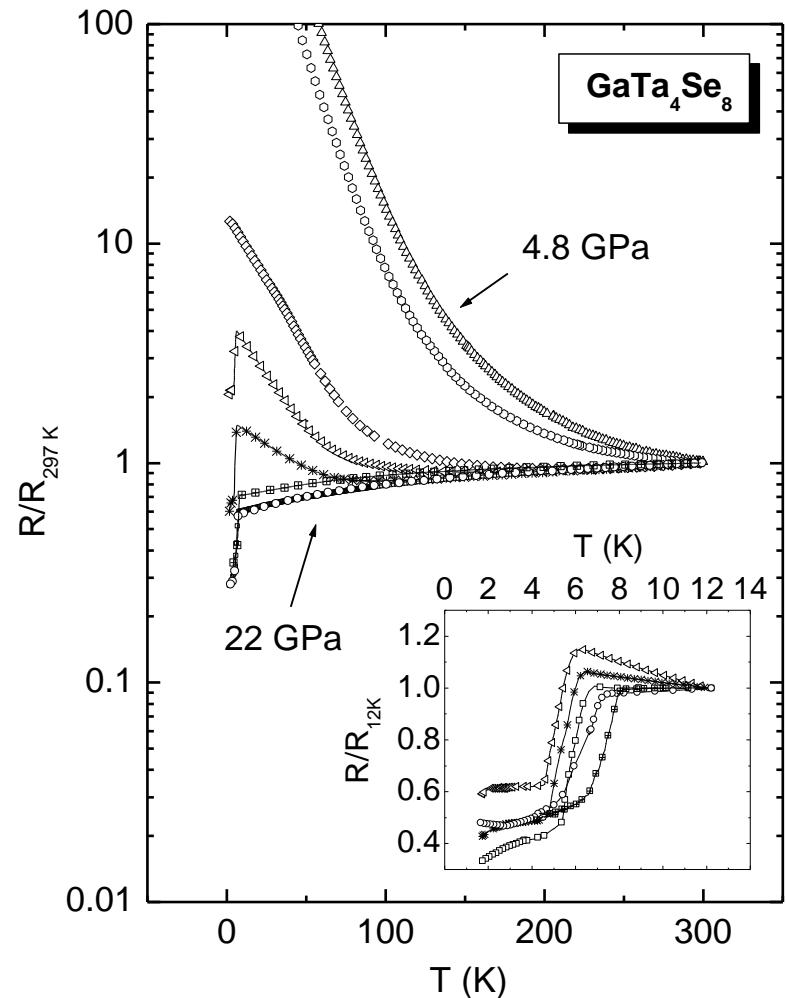
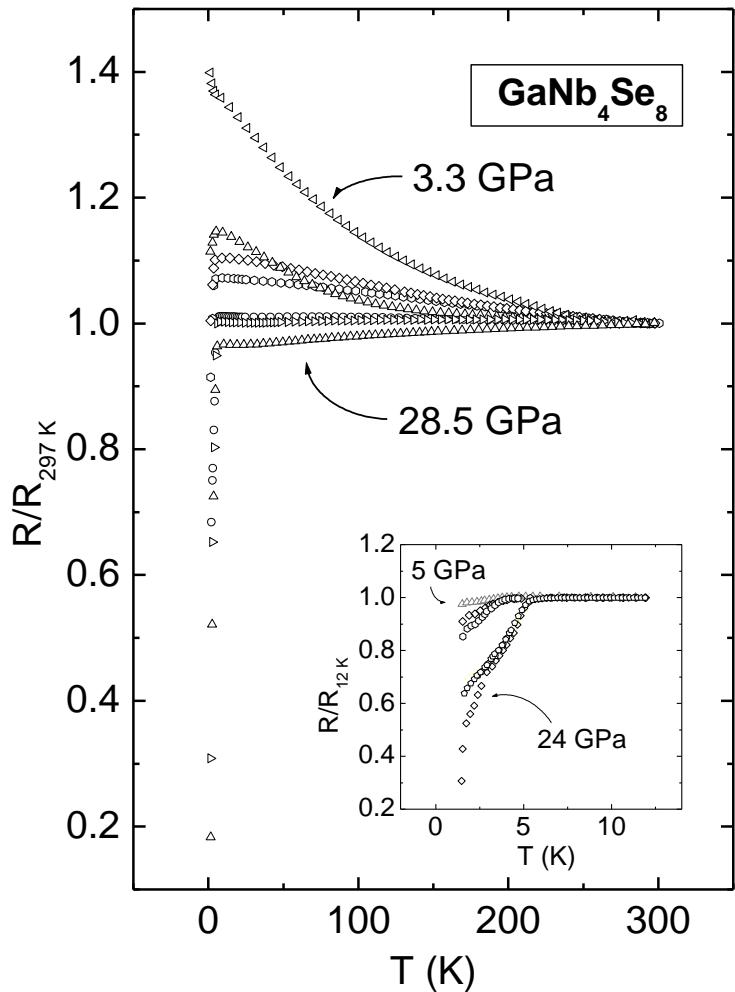
Results at ambient pressure



R. Pocha et al., JACS 2005

- small energy gap $\sim 0.1 \text{ eV}$
- Curie-Weiss behavior ($100 \text{ K} \leq T \leq 300 \text{ K}$), $\Theta_{\text{CW}} = -298 \text{ K}$! Indicating the existence of strong magnetic correlations, but no magnetic ordering is found down to 1.6 K (neutron scattering).
- values of the effective magnetic moments are $1.6 \mu_B$ per Nb_4 -cluster (close to theoretical values $1.73 \mu_B$ for $S = \frac{1}{2}$) and $0.7 \mu_B$ per Ta_4 -cluster.

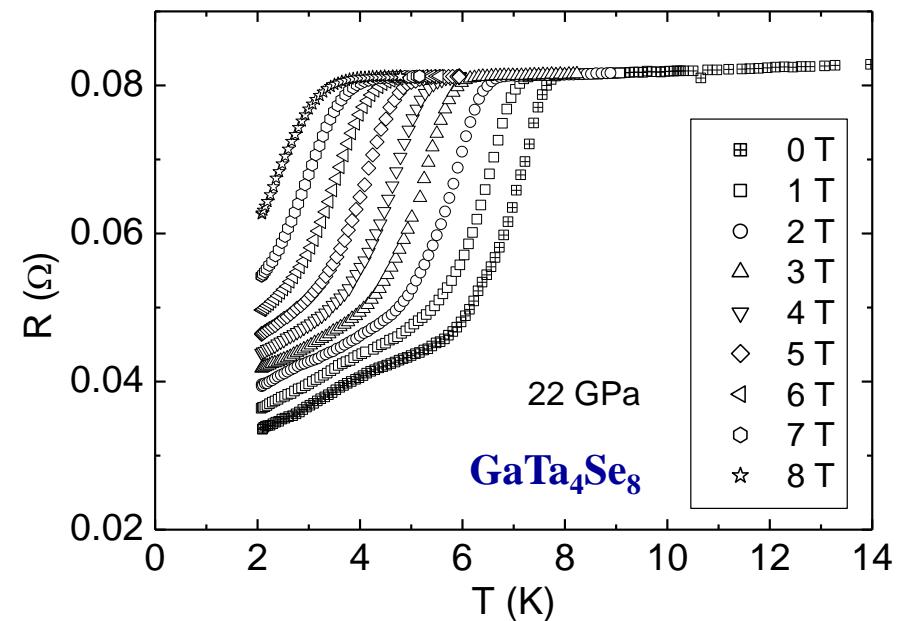
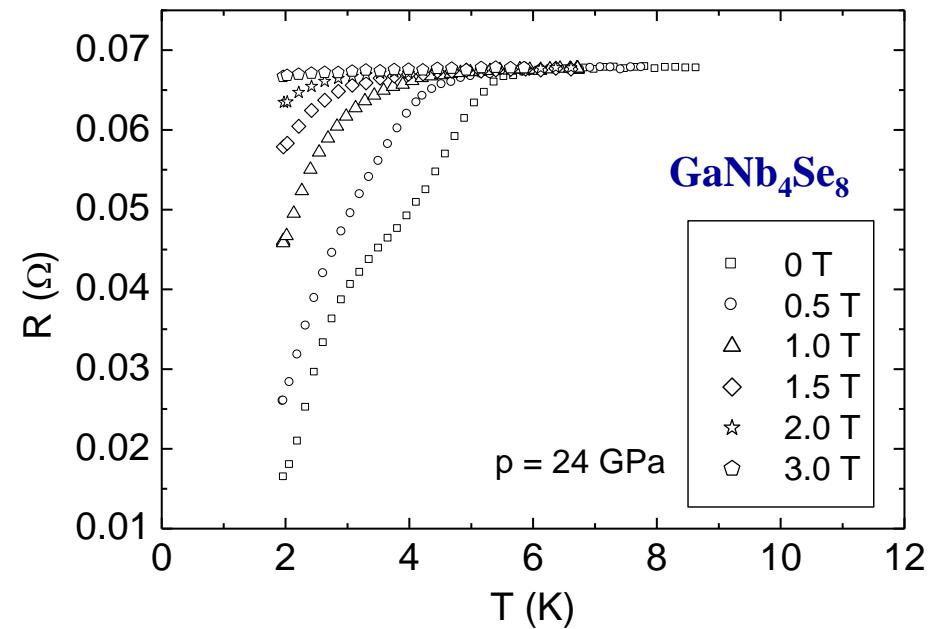
electrical resistance:



Semiconductor-Metal-Transition in GaNb_4Se_8 and GaTa_4Se_8
and superconductivity at high pressures

electrical resistance in magnetic field

⇒ type II superconductor



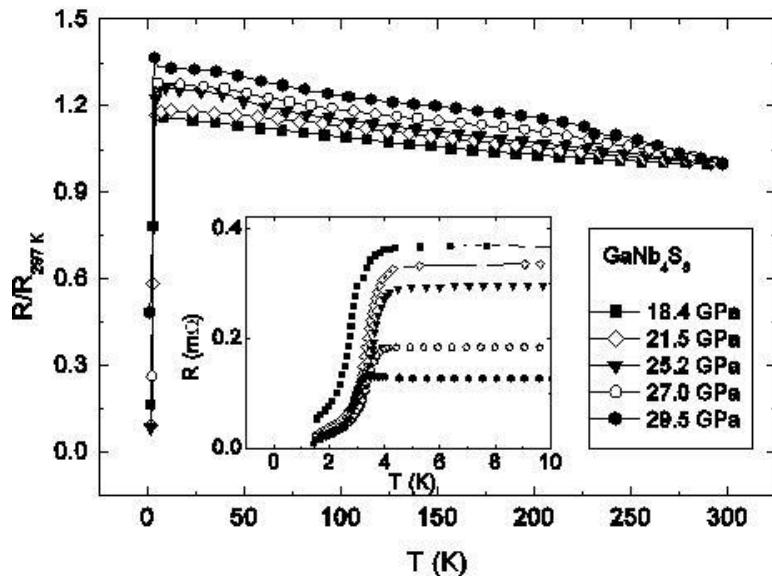
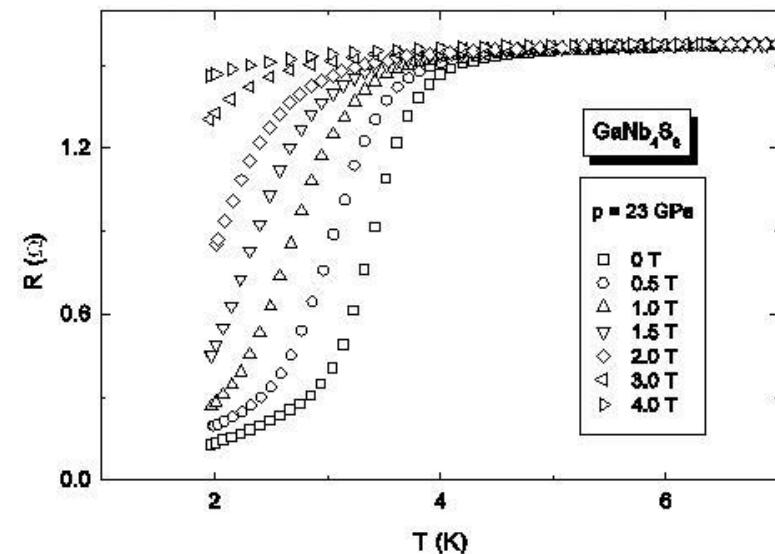
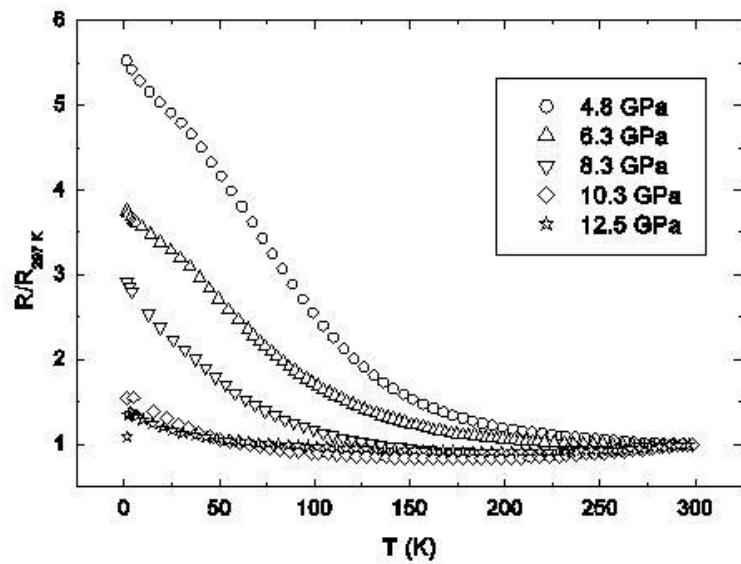
upper critical field $B_{c2} \sim 2 \text{ T}$

coherence lenght $\zeta \sim 130 \text{ \AA}$

upper critical field $B_{c2} \sim 10 \text{ T}$

coherence lenght $\zeta \sim 60 \text{ \AA}$

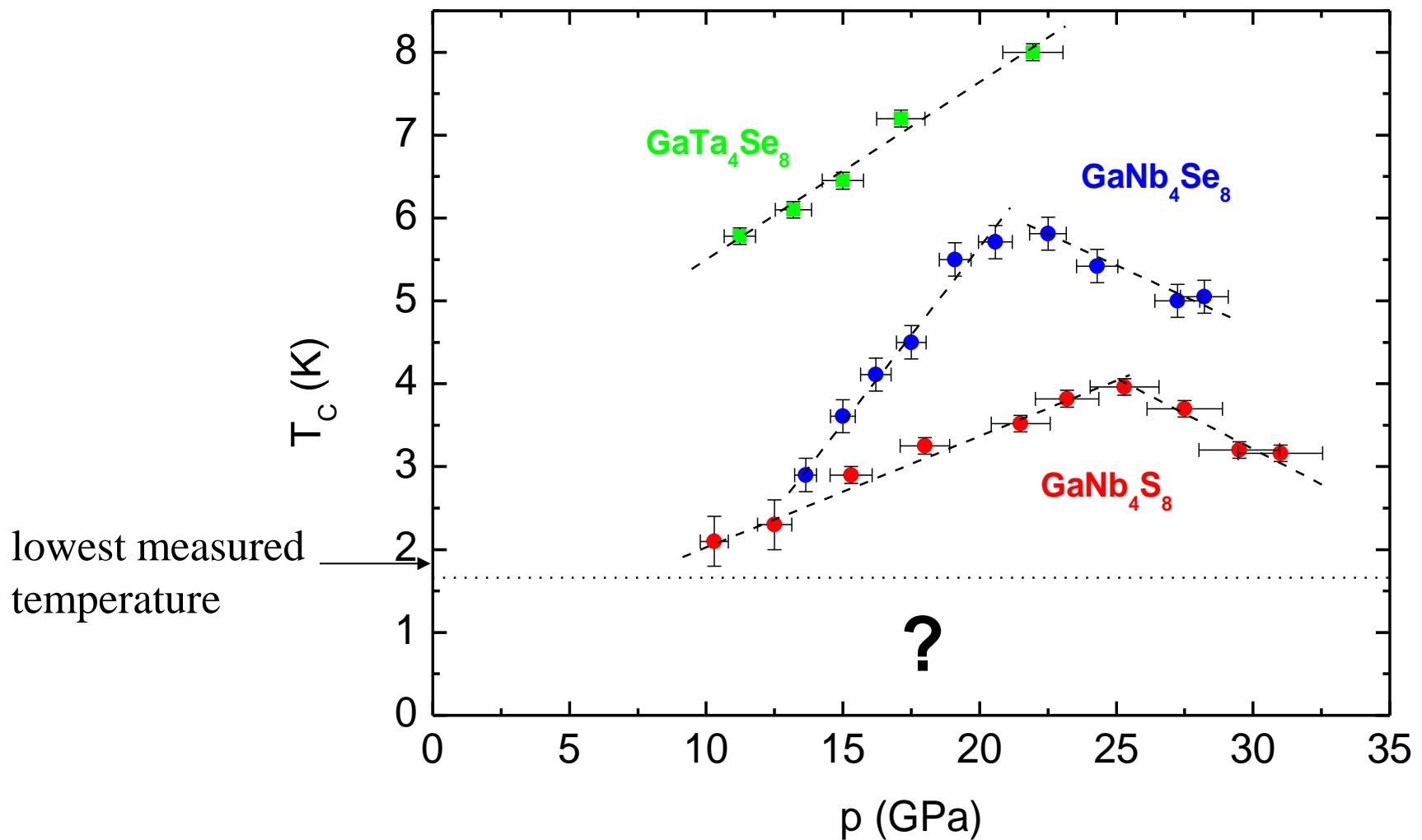
Pressure-induced superconductivity in GaNb_4S_8



upper critical field $B_{c2} \sim 4.5 \text{ T}$

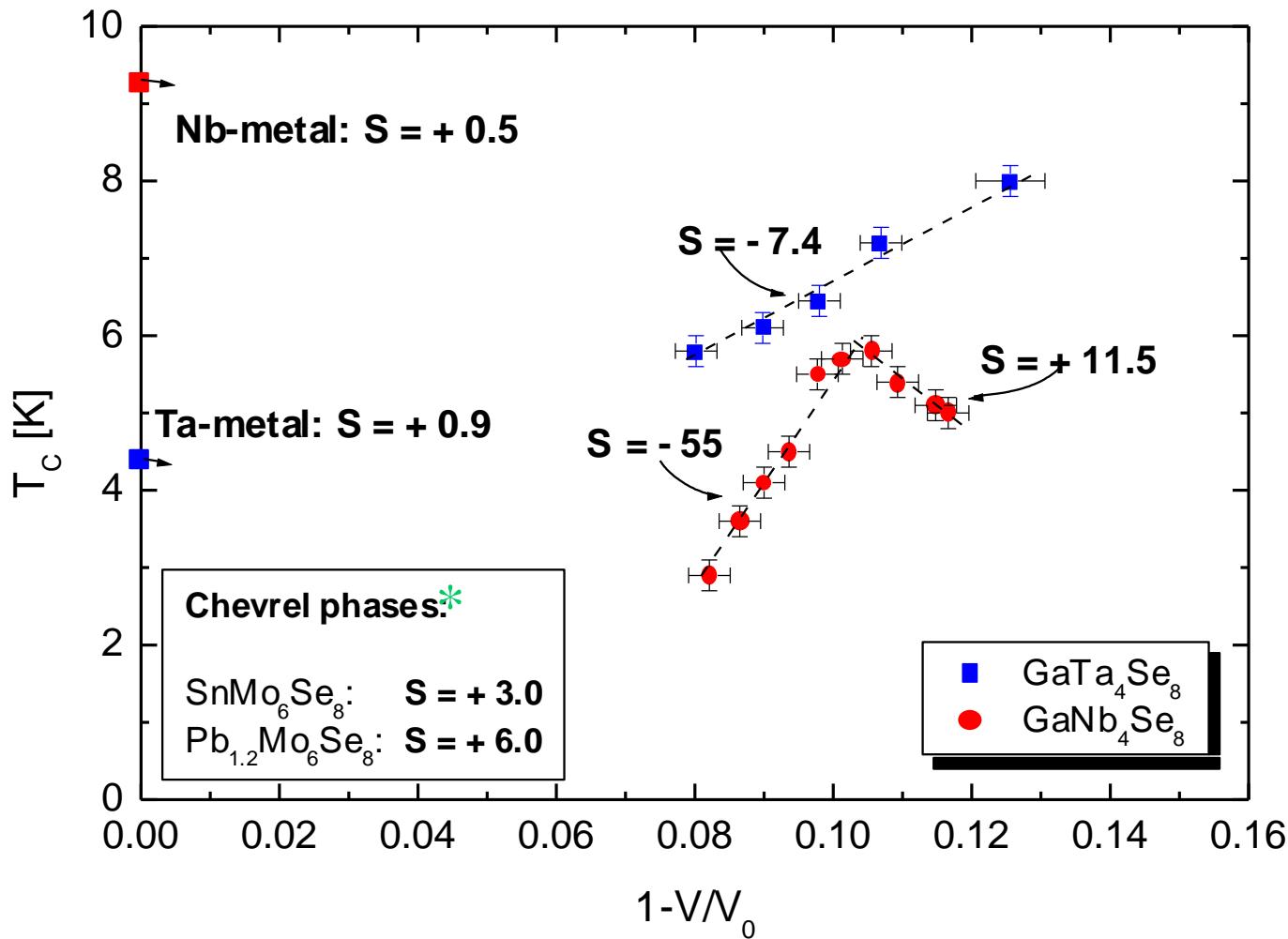
coherence lenght $\zeta \sim 90 \text{ \AA}$

Pressure dependence of T_C



decrease of T_C at higher pressure $p > 20$ GPa is
connected with structural phase transition

volume dependence of T_c

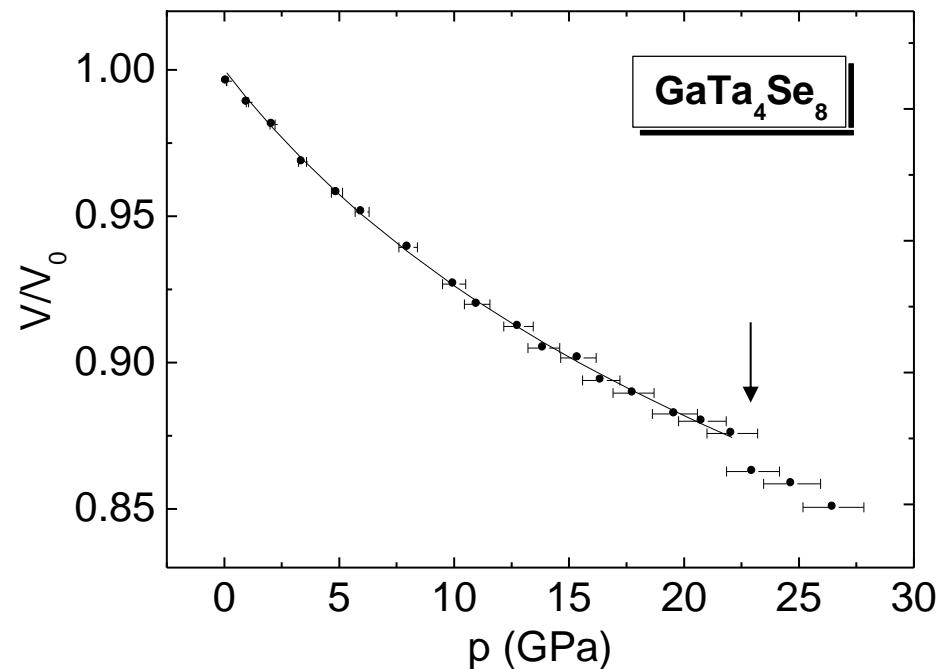
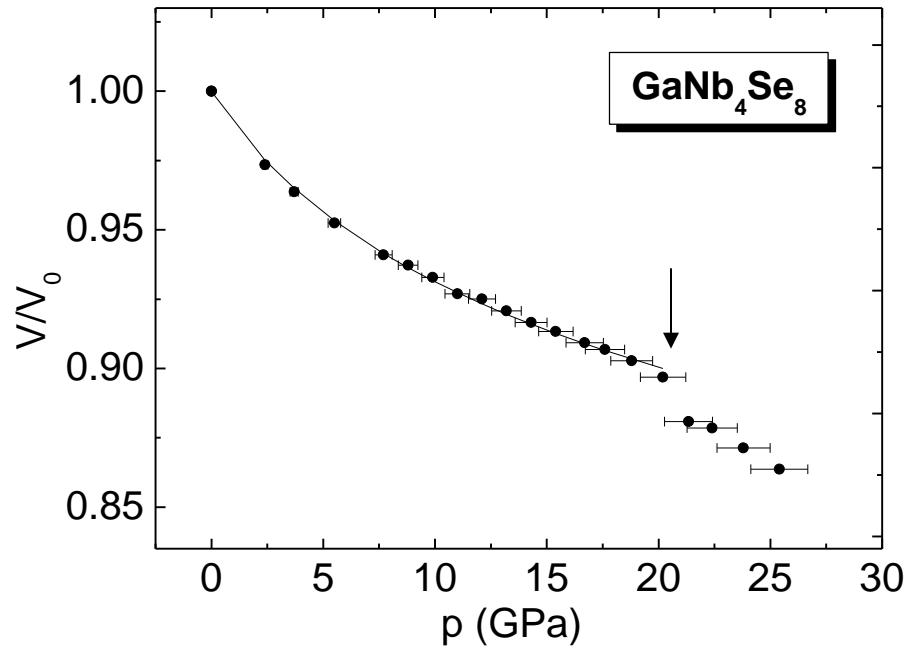


$$S = \frac{\partial \ln T_c}{\partial \ln V}$$

S = Slope

* Calculated from A.W. Webb and R.N. Shelton, J. Phys. F 8, 261 (1978)

Crystal structure at high pressure



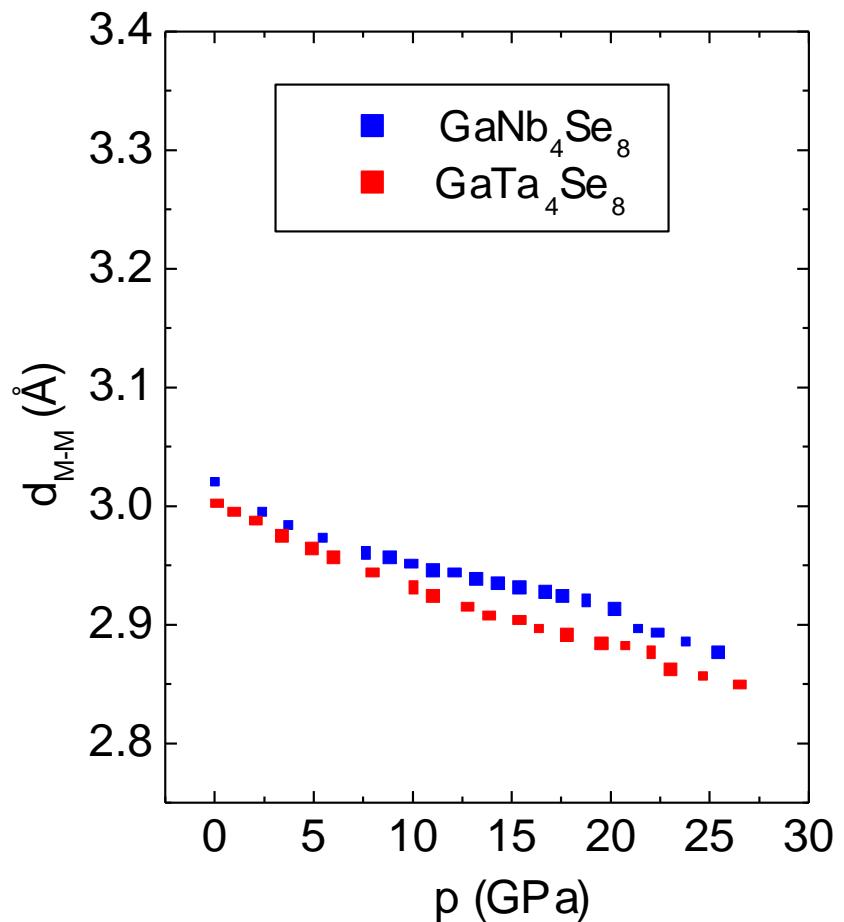
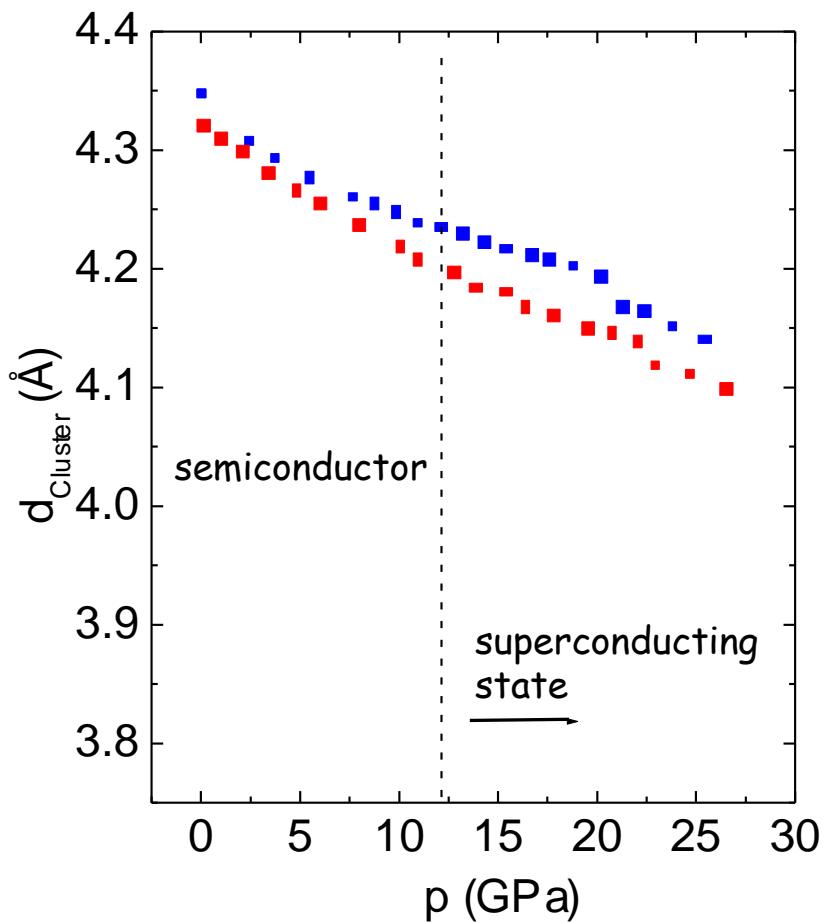
Bulk modulus

$\text{GaNb}_4\text{Se}_8 \quad B_0 = 78(3) \text{ GPa}; \quad B_0' = 15.0(0.6)$

$\text{GaTa}_4\text{Se}_8 \quad B_0 = 98(2) \text{ GPa}; \quad B_0' = 7.2(0.6)$

origin of superconductivity

origin of superconductivity

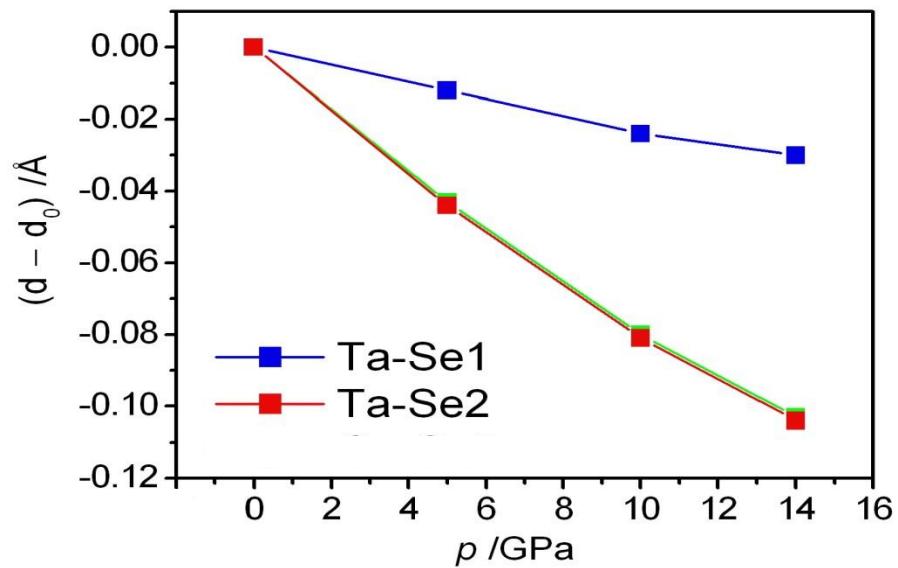
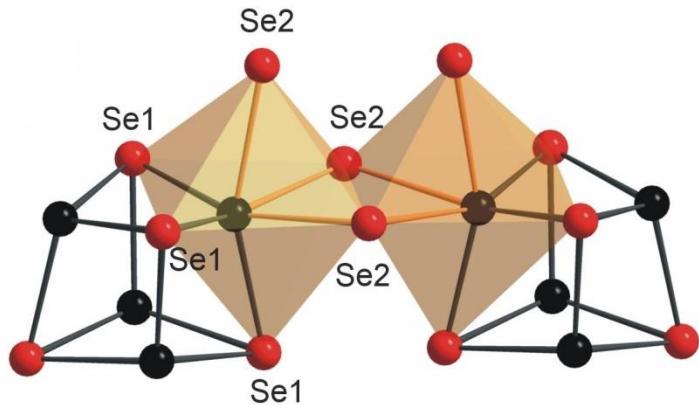


for $p > 10 \text{ GPa}$ $d_{\text{Cluster}} \gg d_{\text{M-M}} !!$



The occurrence of superconductivity is not
related to a decrease of intercluster distances.

Change of local structure at high pressure



Ta atoms move towards the center of the octahedra.



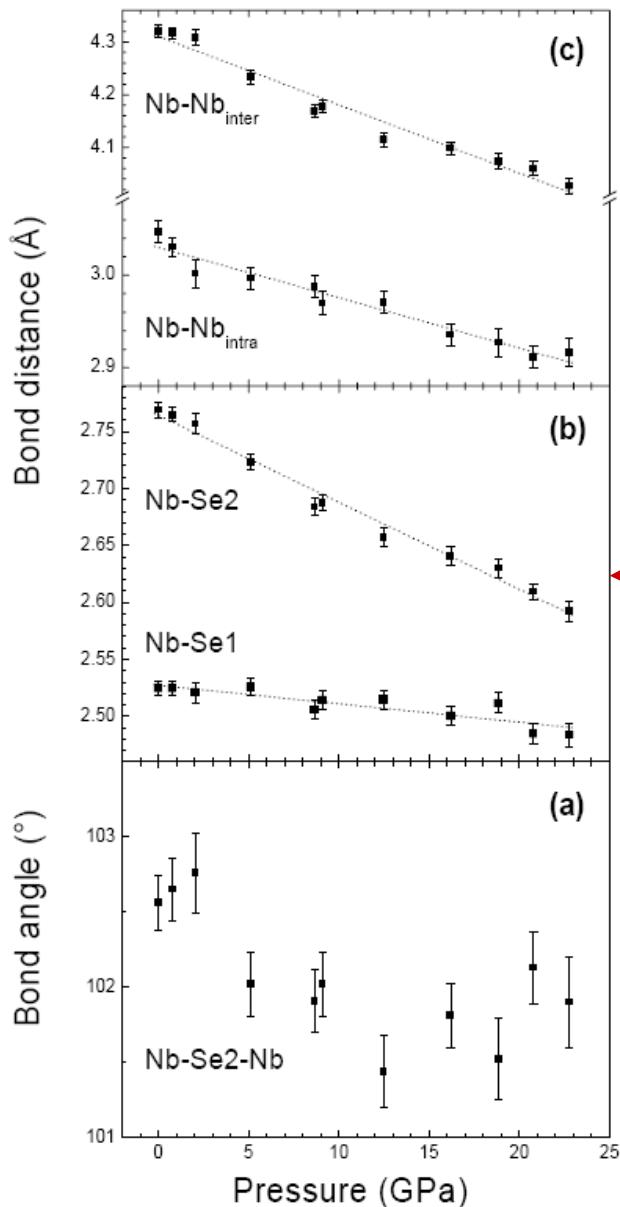
octahedral distortion is strongly reduced by increasing pressure.

Strong increase of the hybridization of the d-states of Ta with p-states of the bridging Se2-ions.



Increase of the effective intercluster coupling → pressure-induced metallic and superconducting state.

Change of local structure at high pressure



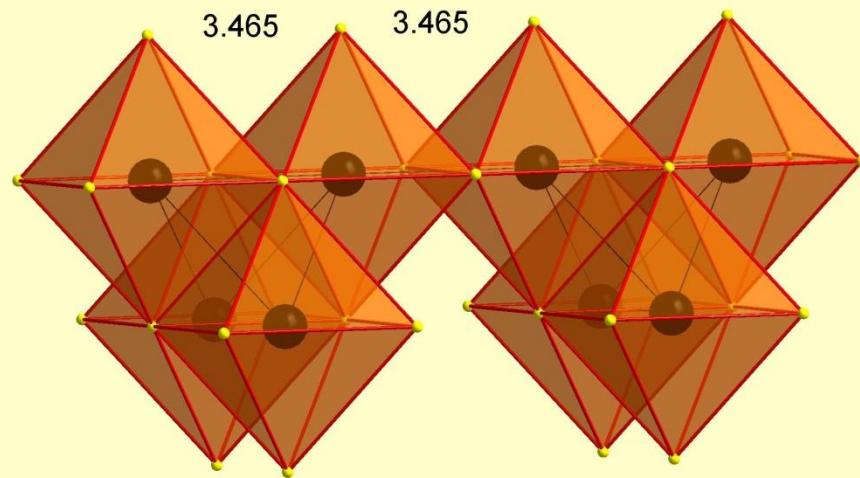
GaNb₄Se₈ - angle resolved x-ray diffraction
(ESRF, Grenoble)

also here: octahedral distortion is strongly reduced by increasing pressure.



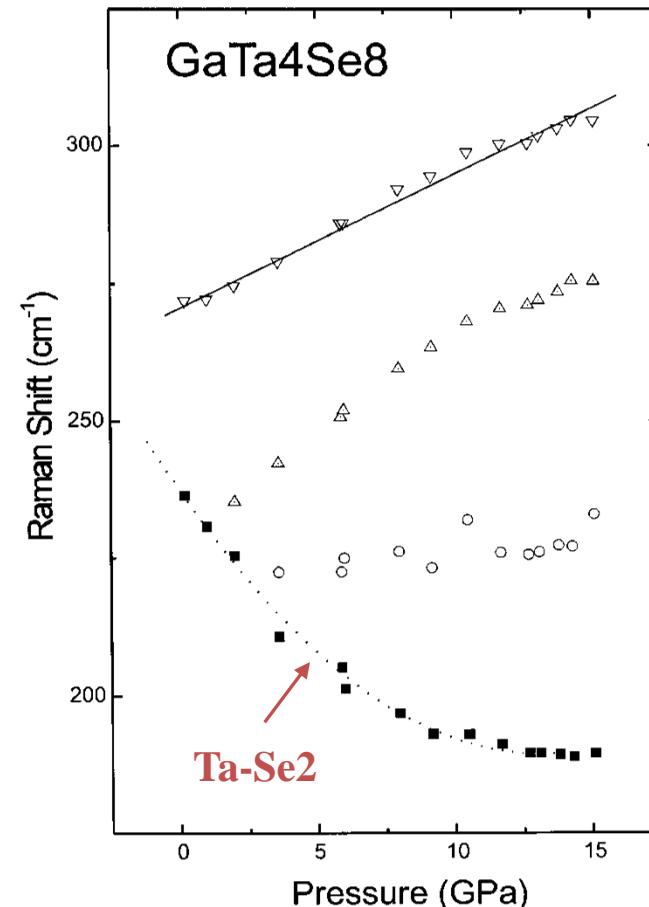
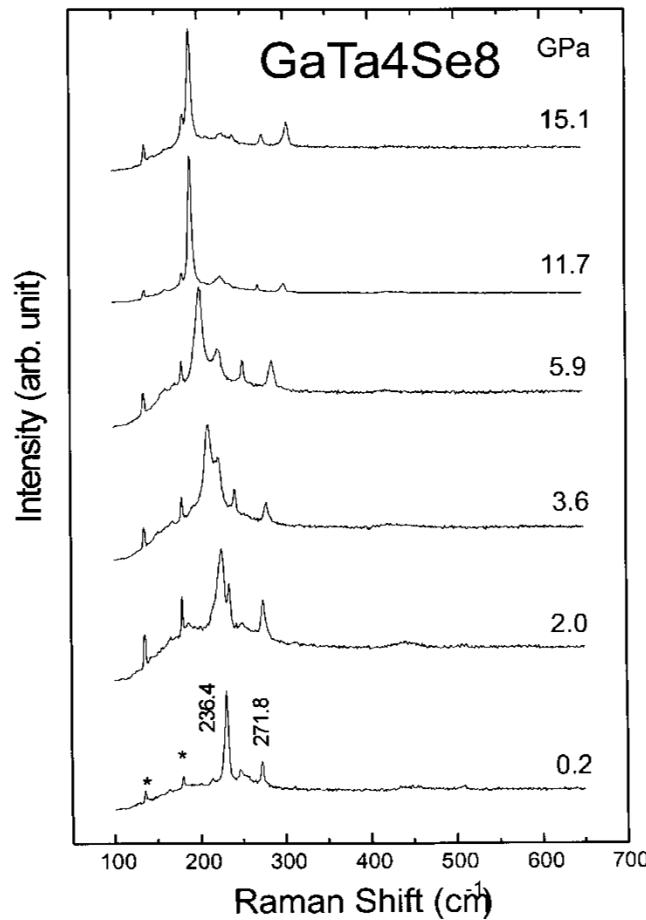
pressure-induced metallic and superconducting state.

X. Wang et al. (to be published)



Lattice dynamics under high pressure

Raman spectra under high pressures



M.M.A. et al., PRL (2004)

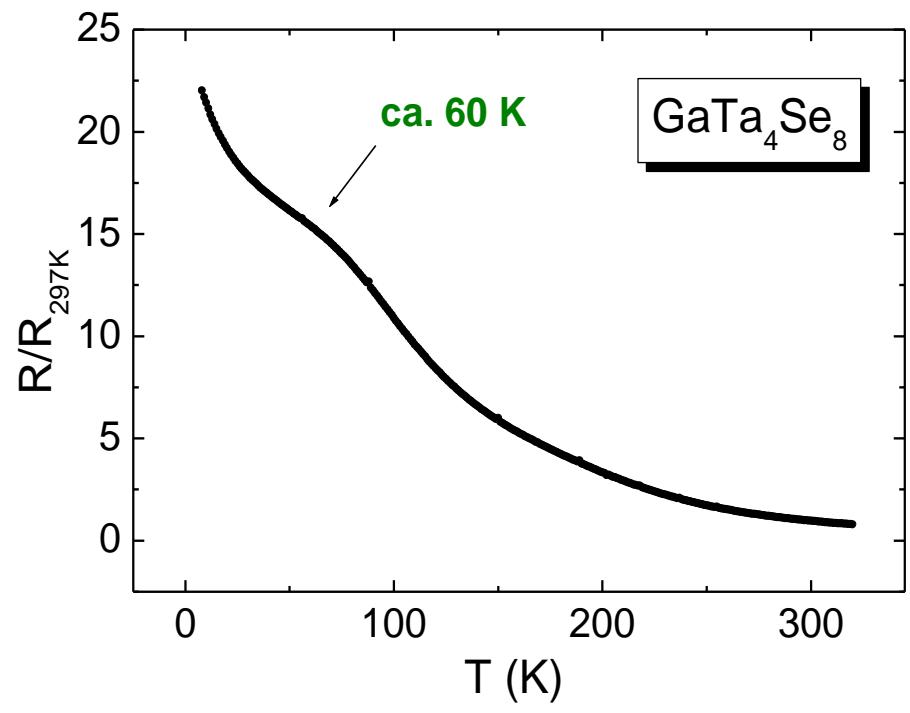
Phonon associated with Ta-Se2 becomes softer by increasing pressure and exhibits finite value at high pressures.

origin of superconductivity

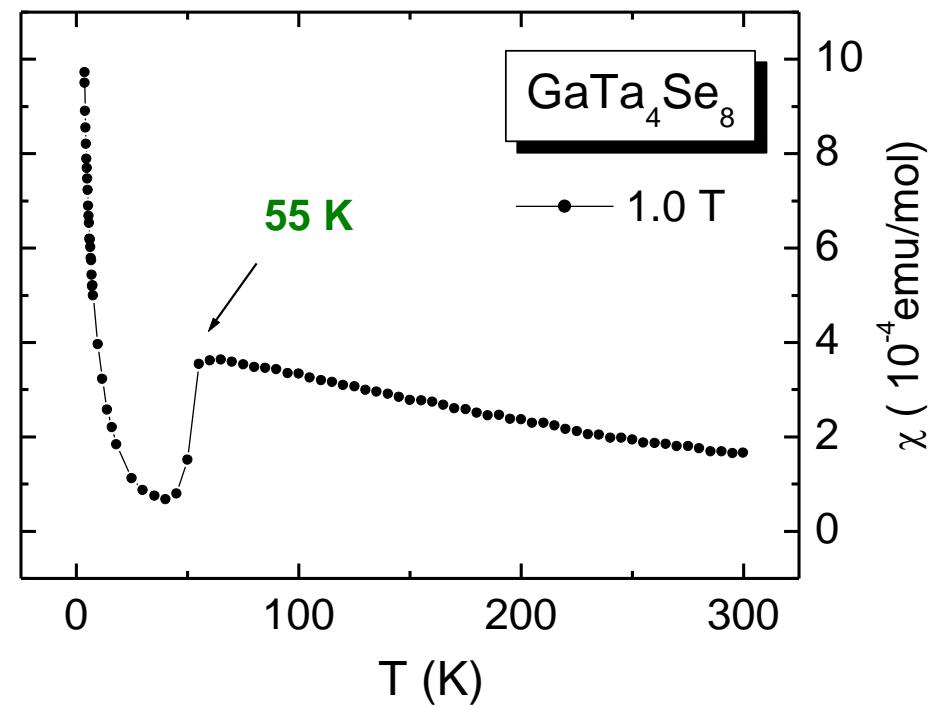
nature of the ground state

Results at ambient pressure:

Electrical resistance



Magnetic susceptibility

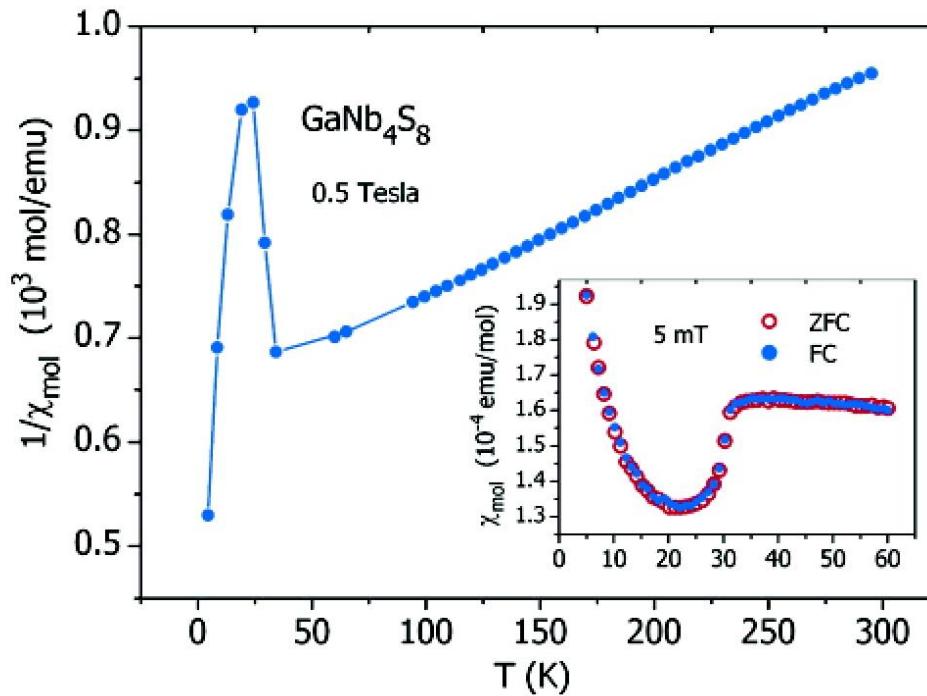


$R(T) \Rightarrow$ small energy gap ~ 0.1 eV

$\chi(T) \Rightarrow$ anomaly at low temperatures;
probably connected with structural distortion?

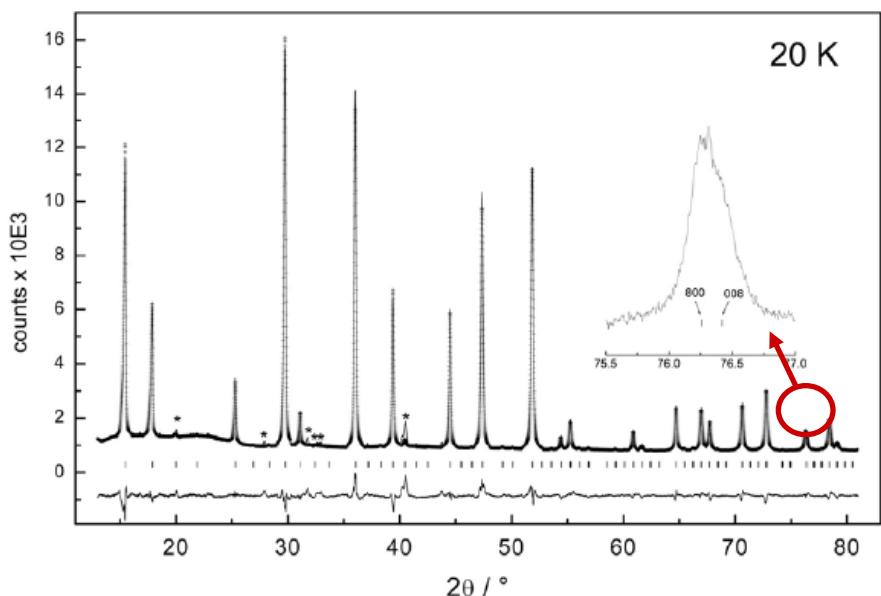
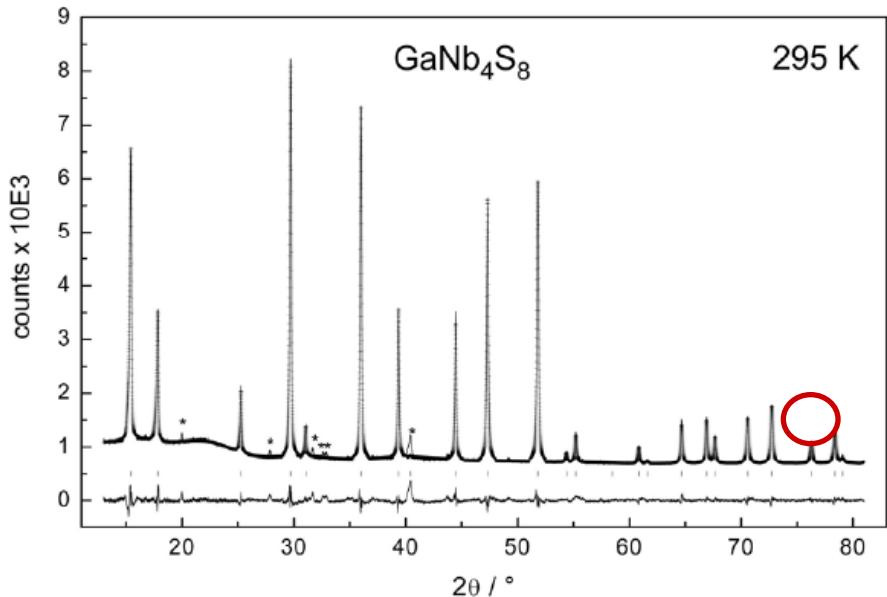
Results at ambient pressure

R. Pocha et al., JACS 2005



Curie-Weiss behavior ($100 \text{ K} \leq T \leq 300 \text{ K}$), $\Theta_{\text{CW}} = -298 \text{ K}$!
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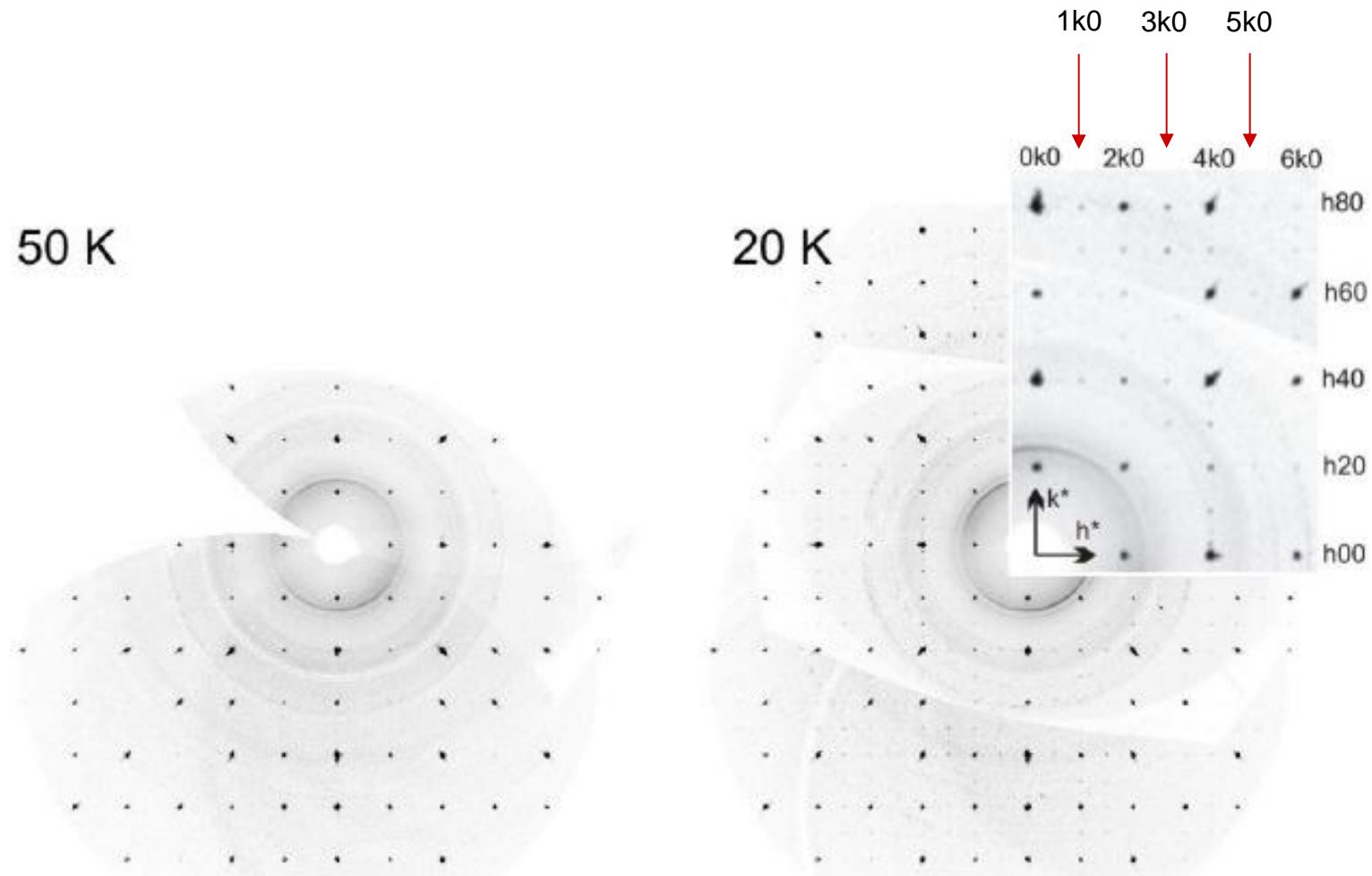
What causes the sharp drop in the susceptibility at about 30 K?



Structural phase transition
below 30 K!

Very small tetragonal distortion
($\text{F}43\text{m} \rightarrow \text{P}42_1\text{m}$).

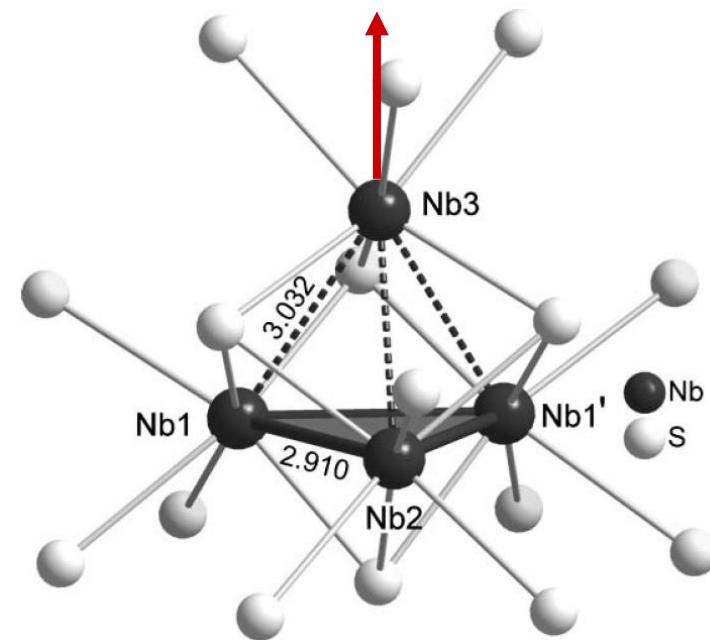
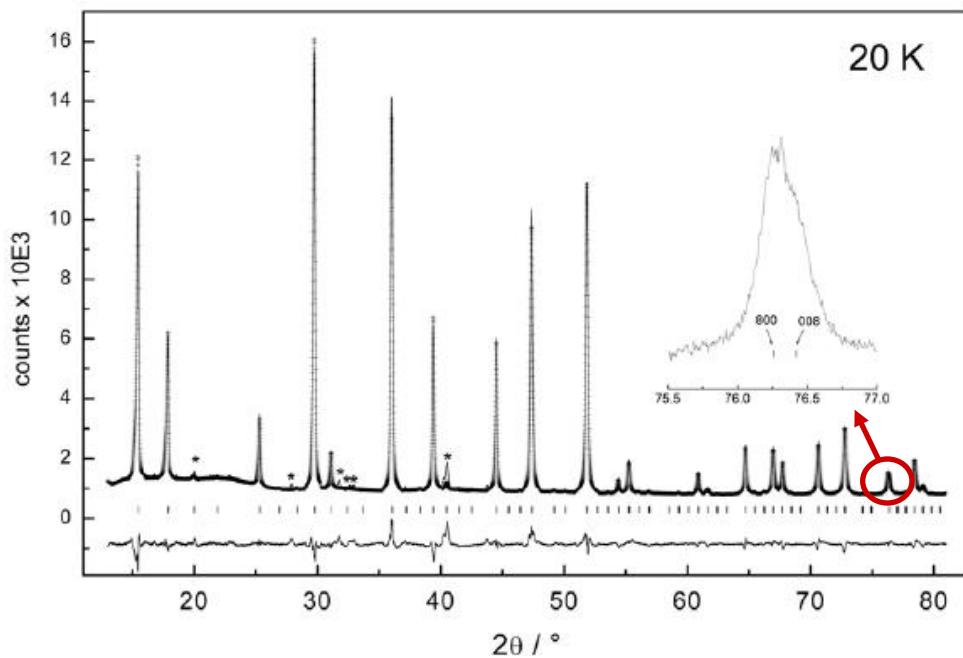
S. Jakob et al., J. Mater. Chem. 2007, 17, 3833 (2007)



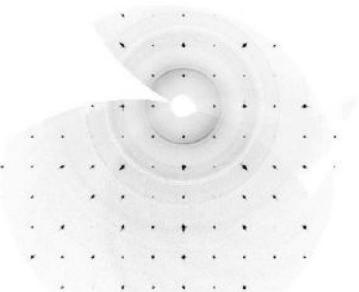
Reciprocal space $hk0$ -sections of GaNb_4S_8 .

S. Jakob et al., J. Mater. Chem. 2007, 17, 3833 (2007)

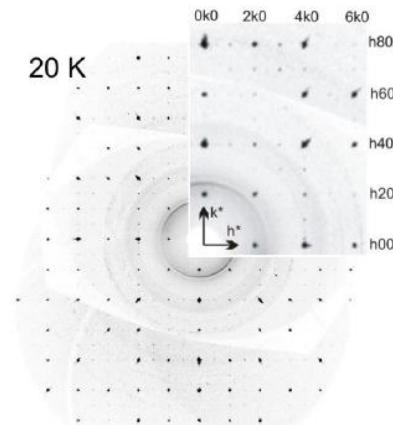
What causes the sharp drop in $\chi(T)$ at about 30 K?



50 K



20 K

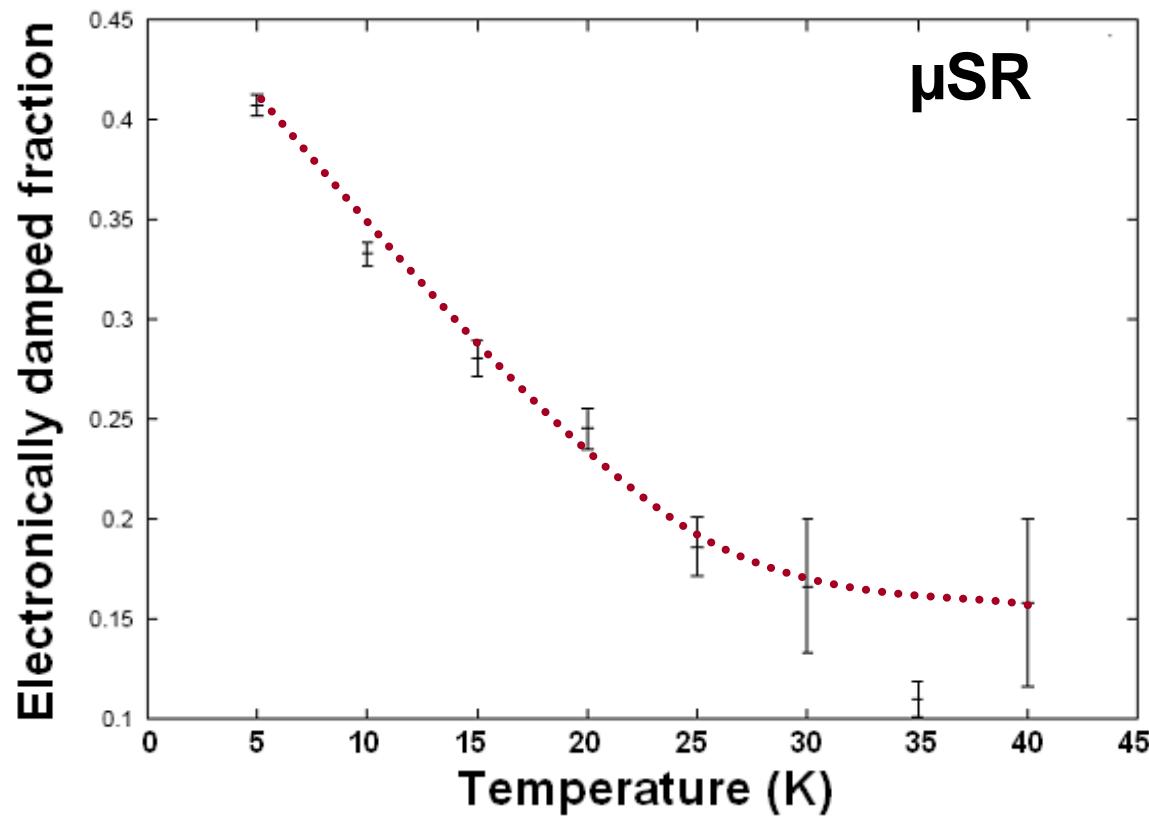


**Structural phase transition
below 30 K!**

Very small tetragonal distortion
(F43m \rightarrow P42₁m).

S. Jakob et al., J. Mater. Chem. 2007, 17, 3833 (2007)

Evidence for magnetic correlations below 30K



Structural phase transition is associated with the appearance of a damped signal fraction below 30 K, indicating magnetic correlations (no long-range static order down at least to 5 K).

Current scenario

